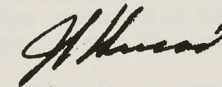


AVRO AIRCRAFT LIMITED
INTER - DEPARTMENTAL MEMORANDUM

Ref 4072/20/J
Date November 4, 1957
To Mr. J. D. Hodge, Technical Flight Test Co-ordinator
From J. Lucas, Chief of Performance Evaluation
Subject PERFORMANCE DATA FROM ARROW 1 FLIGHT TESTS

Attached herewith, please find report 71/PERF/2, Issue 2, on Programming for Performance Data from Arrow 1 Flight Tests. This issue supersedes the original issue of report 71/PERF/2 and includes clarification and refinements to the list of available instrumentation, Sanborn editing records and to the applicable formulae for I.B.M. 704 computations. A note on aircraft weight and C.G. data (Appendix I) is added.

It is realized that performance testing on Arrow 1 aircraft is of secondary importance but useful results are readily obtainable from the existing program using available instrumentation. Adequacy of thrust measuring instrumentation is discussed under report 70/PERF/ 1 App. II.



J. Lucas
Chief of Performance Evaluation.

c.c.
Messrs J. A. Chamberlin
F. Brame
A. J. Downing
D. N. Scard
D. R. Woolley
G. Esilman

Central Files



AVRO AIRCRAFT LIMITED
MALTON - ONTARIO

TECHNICAL DEPARTMENT

REPORT NO. 71/PERF72 Iss. 2

SHEET NO. 1

AIRCRAFT:

ARROW 1

PERFORMANCE FLIGHT TESTS

PREPARED BY

DATE

R. Waechter

Nov/57

CHECKED BY

DATE

PROGRAMMING FOR PERFORMANCE DATA FROM ARROW 1 FLIGHT TESTS INTRODUCTION:-

This report on programming for performance data from Arrow 1 flight tests is divided into three main sections, i.e. 1) Available instrumentation. 2) Sanborn trace recorder for editing and 3) Input - output summary and applicable formulae and charts for I.B.M. 704 computations.

Use is made of available instrumentation, which can be used for obtaining preliminary performance data during the course of Arrow 1 flight testing. Instrumentation accuracy is given in dimensional units with corresponding percent accuracy of full range varying between 0.2% for measured angle of attack to 3.0% for dive brake angle, but generally between 0.5 and 1.0% for all other instrumentation. Standard recording frequency is 20 per second except where noted as continuous. However, overall data processing at 2 per second will suffice with a maximum frequency of 5 per second and a minimum frequency of every 5 seconds when required. Hence before final data processing on the I.B.M. digital computer, the data will need to be transformed to the lower frequencies either on the computer itself or on an intervalometer.

A Sanborn trace recorder will be used to edit the flight test data prior to entering on the I.B.M. 704 computer. This trace recorder will also show traces of all measurements which require no further computations, such as elevator angle, pitch angle, air brake angle etc. This would eliminate the need to enter them on the I.B.M. 704 computer and would simplify programming. It would be desirable to convert ambient (static and dynamic) pressure measurements to indicated Mach number and indicated altitude on the Sanborn recorder to facilitate editing as well as to record accelerations and R.P.M. settings to determine the steadiness of each manoeuvre. A total of 8 traces per record is available, with paper speeds of .25, .5, 1.0, 2.5, 5.0, 10, 25, 50 & 100 mms/sec and a paper length of 200 feet. At the editing stage, time frequencies between 5 seconds intervals and 5 per second will be decided for 704 computations.

Computations will then be made by the 704 computer from which all output will be presented as time plots and tabulated when required, except from steady level speed tests where the stabilized portion will be previously obtained by editing and the computer output tabulated only. Gross plots of computer output data will be made only when specifically requested.

All records should be identified by aircraft number, flight number and run number.



AVRO AIRCRAFT LIMITED
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TECHNICAL DEPARTMENT

REPORT NO. 71/PERF/2 Issue 2

SHEET NO. 2

AIRCRAFT: ARROW 1	PERFORMANCE FLIGHT TESTS	PREPARED BY	DATE
		R. Waechter	Nov. 1957
		CHECKED BY	DATE

SECTION I :- AVAILABLE INSTRUMENTATION

<u>ITEM</u>	<u>RANGE</u>	<u>ACCURACY</u>	<u>REMARKS</u>
1) Time scale	40 min.	+ .01 sec.	
2) Record identification or coding	-	+ .01 sec.	Pending
3) Ambient static pressure	a) 0-2160 psf.	+ 15 psf.)	Require range selector.
	b) 0-720 psf.	+ 5 psf.)	
	c) 0-288 psf.	+ 2 psf.)	
4) Ambient differential pressure	a) 0-2880 psf.	+ 20 psf.)	Require range selector.
	b) 0-1440 psf.	+ 10 psf.)	
	c) 0-720 psf.	+ 5 psf.)	
5) O.A.T _M	-65 + 350°F	+ 2°F	
6) Longitudinal acceleration	+ 1g	+ .01g	Parallel to fuselage datum.
7) Lateral acceleration	+ 1g	+ .01g	Continuous recording (and telemetered).
8) Normal acceleration	-3 + 8 g	+ .05g	Continuous recording (and telemetered).
9) Angle of attack (α)	-10 + 40°	+ .1°	Continuous recording.
10) Angle of pitch (θ) complete range	+ 60°	+ 0.5°	
sensitive range *	+ 10°	+ 0.1°	
11) Rate of change of pitch ($\dot{\theta}$)	+ 30°/sec.	+ .30°/sec.	Continuous recording.
12) Elevator angle (port and stbd.)	-30 + 20°	+ .3°	Continuous recording.
	+ 10°	+ .1°	
13) Air brake angle (port and stbd.)	0 to 60°	+ 2°	Only port or stbd. required *
14) L.P.Comp.R.P.M.(N ₁) (port and stbd.)	0 - 110%	+ .5%	
15) H.P.Comp.R.P.M.(N ₂) (port and stbd.)	0 - 110%	+ .5%	
16) Engine fuel flow (port and stbd.)	600-25,000 ^{lb} hr	+ 125 ^{lb} hr.	Maximum range value could be reduced to 40,000 lbs. for better accuracy.
17) A/B fuel flow (port and stbd.)	500-65000 ^{lb} hr	+ 650 ^{lb} hr.	



AVRO AIRCRAFT LIMITED
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REPORT NO. 71/PERF/2 Iss 2

SHEET NO. 3

AIRCRAFT:

ARROW I

PERFORMANCE FLIGHT
TESTS

PREPARED BY

DATE

R. Waachter

Sept. 1957.

CHECKED BY

DATE

ITEM	RANGE	ACCURACY	REMARKS
18) Fuel remaining, per tank (14 off)	0-300 gals each (max.)	+ 6 gals (max.)	
19) Engine intake P ₂ (port and stbd)	0-30 psia	+ .3 psi	Representative probes after rake calibration.
20) Engine intake p ₂ (port and stbd)	"	"	
21) Engine intake T ₂ (port and stbd) optional	-75+350°F	+ 4°F	May substitute free stream T.
22) Turbine discharge P ₇ (port and stbd)	0-45 psia	+ .45 psi	Manifolded rake measurements.
23) Turbine discharge T ₇ (port and stbd)	0-1400°F	+ 14°F	
24) By-pass gills shut ind. lights, 2 off (port and stbd) (one on side gills and one on oil cooler gill)		shut -not shut and shut and fully open	
25) By-pass temp. above and below jet pipe T _B (port)	0-500°F	+ 5°F	
26) By-pass press. below mid jet pipe P _B (port)	0-35 psia	+ .35 psi	Static pressure measurement here assumed = downstream total press.
27) Diff. static in lower ejector just upstream of final nozzle, relative to ambient static (port) (p _B - p ₁)	-3 to 0 psig	+ .05 psi	
28) By-pass temp. above and below turbine (port) *	0-500°F	+ 5°F	Of incidental use only, in performance measurements.
29) By-pass static press. above rear comp. (port) *	0-35 psia	+ .35 psi	

NOTE:- Items 25, 26 and 27 are available on port side only and will be assumed identical on starboard side.

Item denoted thus *, are not required for the program as detailed herein but should be available if and when needed.

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MALTON, ONTARIO

TECHNICAL DEPARTMENT

REPORT No. 71/PERF/2 Iss. 2

SHEET No. 4

AIRCRAFT:

ARROW I

PERFORMANCE
FLIGHT TESTS

PREPARED BY

DATE

R. Waechter

Sept. 1957

CHECKED BY

DATE

SECTION II :- SANBORN EDITING RECORDS

Sanborn trace records will consist of a time history of direct measurements for editing purposes and recording data which requires no further computation. These traces should be recorded versus time to within $\pm .01$ sec. such that accurate correlation with succeeding I.B.M. 704 records can be made. Overall accuracy to Sanborn trace output, including instrument measuring accuracy, should be within $\pm 2\%$ of full scale reading. In the case of ambient pressure measurements the most sensitive reading should be selected for recording and if conveniently possible they should be converted to traces of indicated Mach number and indicated altitude using the following formulae.

$$\left(\frac{P_T}{p}\right)_i = (1 + .2 M_i^2)^{3.5} \quad \text{for} \left(\frac{P_T}{p}\right)_i \leq 1.894$$

$$\left(\frac{P_T}{p}\right)_i = (1 + .2 M_i^2)^{3.5} \times \left[\frac{1}{\left(\frac{M_i^2 + 5}{6 M_i^2}\right)^{1.4} \left(\frac{7 M_i^2 - 1}{6}\right)} \right]^{2.5}$$

$$\text{for} \left(\frac{P_T}{p}\right)_i > 1.894$$

$$H_i = 145,447 \left[1 - \left(\frac{p_i}{2116}\right)^{0.1903} \right] \quad \text{for} p_i \geq 472.7 \text{ psf}$$

$$H_i = 164,221 - 47,907 \log p_i \quad \text{for} p_i < 472.7 \text{ psf}$$



AVRO AIRCRAFT LIMITED
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TECHNICAL DEPARTMENT

REPORT NO. 71/PERF/2 Iss.2

SHEET No. 5

AIRCRAFT:

ARROW 1

PERFORMANCE
FLIGHT TESTS

PREPARED BY

DATE

R. Waechter

Oct. 1957

CHECKED BY

DATE

Two Sanborn records, consisting of 8 items each, are required i.e.

- | | | |
|--|---|---|
| 1. a) Ambient static pressure P_1 | } | convert to M_1 and H_1
if conveniently
possible |
| b) Ambient dynamic pressure $q_{c1} = P_{T1} - p_1$ | | |
| c) H.P.compressor R.P.M., port N_{2p} | | |
| d) H.P.compressor R.P.M., stbd. N_{2s} | | |
| e) Afterburner fuel flow rate, port $(Q_{A/B})_p$ | | (for A/B on or off
indication only) |
| f) Normal acceleration | } | as measured relative A/C
datums |
| g) Longitudinal acceleration | | |
| h) Lateral acceleration | | |
| 2. a) Angle of pitch | | |
| b) Air brake angle | | |
| c) By-pass gill position (port and stbd) shut-not shut indications | | |
| d) Oil cooler gill (port and stbd) shut and fully open indications | | |
| e) Elevator angle (complete range, port) | | |
| f) Elevator angle (sensitive range, port) | | |
| g) Elevator angle (complete range, stbd.) | | |
| h) Elevator angle (sensitive range, stbd.) | | |

The first record will be used for editing and thereafter for reference only, while the second record will be used in conjunction with I.B.M. 704 computer output data.

Some identification signal should be available on the Sanborn records where the pilot has noted the start and/or finish of a test. This signal may be obtained from the pilot's voice recording or from a pilot's coding button. When this identification signal is made available it may replace item 2 h.) on the Sanborn records.



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TECHNICAL DEPARTMENT

REPORT NO. 71/PERF/2 Iss.2

SHEET NO. 6

AIRCRAFT:

ARROW 1

PERFORMANCE
FLIGHT TESTS

PREPARED BY

DATE

R. Wechter

Nov. 1957

CHECKED BY

DATE

SECTION III:- INPUT -OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 704 COMPUTER

In general, I.B.M. 704 computer output will be presented graphically versus time except when specifically requested to be tabulated or be cross plotted. Graphical presentation will be made with 4 outputs versus time on one graph and therefore the following input - output summary is grouped such that each successive 4 outputs are related and will appear on one graph.

Reading accuracy of time scale should be $\pm .01$ seconds

Engine Symbols used are such that

capital P	=	total pressure
small p	=	static pressure
capital T	=	Total Temperature
subscript P	=	port
" S	=	stbd.
" N	=	net thrust
" G	=	gross thrust
F	=	installed engine thrust
X	=	basic or primary engine thrust
subscript O	=	free stream static (or initial conditions)
" 1	=	station 1, free stream total
" 2	=	station 2, engine face
" 7	=	station 7, turbine outlet
" 10	=	station 10, final nozzle (primary)
" B	=	station 10, in by-pass
no subscript	=	free stream conditions

All instrument calibrations, which are in the form of "Y = a x + b" conversions from electrical signal to the required units, are taken for granted in the overall data processing, either prior to entering on the 704 computer or on the computer itself.

- It is assumed that
- acceleration measurements are converted to "g" units
 - ambient pressure measurements are converted to psf
 - engine inlet, turbine outlet and bypass pressure measurements are converted to psi
 - all temperature measurements (ambient and in and around engine) are converted to $^{\circ}$ K.

Hence ensuring formulae are derived using the above units. Where outputs such as L/p , F_N/p , D/p etc are required in units of square inches, conversions are made by appropriate constants in the applicable formulae.

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 704 C

<u>INPUT</u>		<u>OUTPUT</u>	<u>APPLICAB</u>
0.)	Time (T)		
1)	Differential Pressure ($P_{T_i} - p_i$) 0-2380, 1440 and 720 psf		a) Select
	}		b) Determini
2)		Ambient Static Pressure p_i 0-2160, 720 and 288 psf	c) Determini
		1a)	M
			d) Determini
			or $\frac{P_T}{p} =$
			e) Determini
			$\frac{\Delta p}{P_i}$
			$p = P_i$
		1(b)	H_p (ft)
			f) determini
			$H_p = 145$
			$H_p = 164$
		1(c)	R_{O_1}
			$R_{O_1} = (1$

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

- a) Select reading of greatest sensitivity
- b) Determine P_{T_i}/P_i
- c) Determine $P_{T/p}$ Chart I $\Delta \left(\frac{P_{T_i}}{P_i} \right)$ vs R_{T_i}/P_i
 Chart II $\Delta \left(\frac{P_T}{P_i} \right)$ vs R_T/P_i
- d) Determine M from $P_{T/p} = (1 + .2M^2)^{3.5}$

$$\text{or } \frac{P_T}{P} \approx (1 + .2M^2)^{3.5} \left[\frac{1}{\left(\frac{M^2 + 5}{6M^2} \right)^{1.4} \left(\frac{7M^2 - 1}{6} \right)} \right]^{2.5}$$

- e) Determine p using chart II
$$\frac{\Delta p}{P_i} = \frac{-\Delta \left(\frac{P_T}{P_i} \right)}{\frac{P_T}{P_i}}$$

$$p = P_i + \left(\frac{\Delta p}{P_i} \right) P_i$$

- f) determine H_p
$$H_p = 145,447 \left[1 - \left(\frac{p}{2116} \right)^{0.1903} \right]$$

$$H_p = 164,221 - 47,907 \log p$$

$$R_{P_i} = (1 + .2M^2)^{3.5}$$

Pitot correction (unique curve)

Static correction (unique curve)

$$P_{T/p} \leq 1.894$$

$$P_{T/p} > 1.894$$

$$\left. \begin{array}{l} p \geq 472.7 \text{ psf.} \\ p < 472.7 \text{ psf.} \end{array} \right\} \text{ I.C.A.O.}$$

Ref: NACA TR 1235

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.E.M. 704

<u>INPUT</u>		<u>OUTPUT</u>		<u>APPLI</u>
3.	Amb. air temp $T_M^{\circ K}$	1 (d)	$T_0^{\circ K}$	$T_0 = T_M$
		2 (a)	$P_1 \sqrt{T_1}$	$P_1 \sqrt{T_1}$
		2(b)	$(R/C)_1$ (fpm)	$(R/C)_1$
		2(c)	$(R/C)_2$ (fpm)	$(R/C)_2$
		2(d)	$\frac{R/C}{V_0}$	$\frac{R/C}{V_0} =$
4.	Angle of pitch θ deg.			
5.	Rate of pitch $q = \dot{\theta}$ deg/sec			
6.	Angle of attack α_i	3(a)	Angle of attack α	$\alpha = \alpha_i$
7.	Normal accel. a_{Ni} (g units)	3(b)	Normal accel a_N	$a_N = [a_{Ni} + 1]$
8.	Long. accel a_{Li} (g units)	3(c)	Long accel a_L	$a_L = [a_{Li} - 1]$
9.	Fuel remain. (14 tanks)			F_1 and
10(a)	Operational weight empty = W_0			F_3, F_4
10(b)	C.G. position (C.G.) ₀ % M.A.C. at W_0 , H/C up, water methonal and alcohol tanks full	3(d)	C.G. % M.A.C. (H/C up)	C.G. =

FLIGHT TESTS

FORMS OR CHARTS FOR I.B.M. 704 COMPUTER

SHEET NO. 8
 DATE Sept. 1957

REPORT NO. 11-1000-1-158
 PREP. BY R. WAECHTER

APPLICABLE FORMULAE, OPERATION OR CHART	REMARKS
$T_o = T_M / (1 + .2KM^2)$	K = constant, initially = 1
$P_1 \sqrt{T_1} = \frac{R_{o1} p \sqrt{T_o (1 + .2M^2)}}{144}$ $(R/C)_1 \text{ fpm} = \frac{\Delta \text{ Hp (ft)}}{\Delta T \text{ (secs)}} \times 60$ $(R/C)_2 \text{ fpm} = 4030 \frac{\Delta (M^2 T_o)}{\Delta T \text{ (secs)}}$ $\frac{R/C}{\sqrt{\theta}} = \frac{(R/C)_1 + (R/C)_2}{\sqrt{T_o/288}}$	Non steady level flight only Note: - $\frac{(R/C)_2}{M \sqrt{T_o}} \approx 3945 \times a_L$ for a_L in 'g' units
$\alpha = \alpha_i + \Delta \alpha - \frac{g(X - X_{C.G.})}{3765 M \sqrt{T_o}}$ $a_N = [a_{Ni} - \cos \theta] \times \cos \alpha + [a_{Li} - \sin \theta] \times \sin \alpha$ $a_L = [a_{Li} - \sin \theta] \times \cos \alpha - [a_{Ni} - \cos \theta] \times \sin \alpha$ <p>F_1 and F_2 = fuselage tanks fuel remain, (Lbs.)</p> <p>$F_3, F_4, F_5, F_6, F_7,$ and F_8 = wing tanks (port + stbd) fuel remain (Lbs.)</p> $C.G. = W_{Ox}(C.G.)_O - 22.5 F_1 - 0.5 F_2 + 2.8 F_3 + 1.4 F_4 + 31.2 F_5 + 42.3 F_6 + 52.8 F_7 + 66.0 F_8$ $W_{Ox} \approx \sum F$	$\theta \approx$ fus. datum rel. horizontal $\Delta \alpha = \text{corr}^n$ for bending & upwash $(X - X_{C.G.}) = \text{vane distance from C.G.} = 45.8 \text{ feet}$ Inputs relative to A/C datum Outputs relative to flight path. See P/AERO DATA/92 Iss. 2 for pitch rate corrections if instrumentation not at C.G. } negligible } useable fuel only

See Appendix I

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 704

INPUT		OUTPUT		APPLIC
		4(a)	$\frac{nW}{P}$	$\frac{M}{P}$
		4(b)	C_{LW}	C_{LW}
		4(c)	C_{LW}^2	
		4(d)	$N_2 / \sqrt{\theta}$	$N_2 / \sqrt{\theta}$
11.	L.P. rpm port $N_{1P1} \%$	5(a)	$N_{1P} / \sqrt{T_1}$	$N_{1P} / \sqrt{T_1}$
12.	L.P. rpm stbd. $N_{1S1} \%$	5(b)	$N_{1S} / \sqrt{T_1}$	$N_{1S} / \sqrt{T_1}$
13.	H.P. rpm port $N_{2P1} \%$	5(c)	$N_{2P} / \sqrt{T_1}$	$N_{2P} / \sqrt{T_1}$
14.	H.P. rpm stbd. $N_{2S1} \%$	5(d)	$N_{2S} / \sqrt{T_1}$	$N_{2S} / \sqrt{T_1}$
15.	Port eng. intake p_{2P} (psi)			
16.	Stbd. eng. intake p_{2S} (psi)			

IGHT TESTS

OR CHARTS FOR I.B.M. 704 COMPUTER

REPORT NO. 9 REPORT NO. 71/PERF/2 ISS. 2
 DATE Nov. 1957 PREP. BY R. Waechter

APPLICABLE FORMULAE, OPERATION OR CHART	REMARKS
$\frac{NW}{p} = \frac{a_N(W_0 + \Sigma F)}{p/144}$ $C_{LW} = \frac{a_N (W_0 + \Sigma F)}{.7 p M^2 S}$ $\frac{N_2/\sqrt{\theta}}{2\sqrt{T_0/233}} = \frac{N_{2P_i} + N_{2S_i}}{2\sqrt{T_0/233}} \times 8732$	<p>S = 1225 sq.ft. wing area = 176,300 sq. inches See output 13(a) and (b) fo thrust corrected values</p>
$\frac{N_{1P}}{\sqrt{T_1}} = \frac{N_{1P_i} \times 6774}{\sqrt{T_0 (1 + .2M^2)}}$ $\frac{N_{1S}}{\sqrt{T_1}} = \frac{N_{1S_i} \times 6774}{\sqrt{T_0 (1 + .2M^2)}}$ $\frac{N_{2P}}{\sqrt{T_1}} = \frac{N_{2P_i} \times 8732}{\sqrt{T_0 (1 + .2M^2)}}$ $\frac{N_{2S}}{\sqrt{T_1}} = \frac{N_{2S_i} \times 8732}{\sqrt{T_0 (1 + .2M^2)}}$	<p>100% $N_1 = 6774$</p> <p>100% $N_2 = 8732$</p>

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 704

<u>INPUT</u>		<u>OUTPUT</u>		<u>APPLIC</u>
17.	Port eng. intake P_{2P} (psi)	6(a)	P_{2P}/P_1	$P_1 = R$ $\frac{1}{T_1}$ $\dot{W}_E = \frac{P}{V}$ Increa $T_1 = T$ $P_1 = R$ $\frac{1}{T}$
18.	Stbd. eng. intake P_{2S} (psi)	6(b)	P_{2S}/P_1	
19.	Port eng. intake T_{2P} ($^{\circ}K$)	6(c)	$\left(\frac{\dot{W}_E \sqrt{T_1}}{P_1} \right)_P$	
20.	Stbd. eng. intake T_{2S} ($^{\circ}K$)			
21.	Turbine Disch. (port) P_{7P} (psi)	7(a)	$(P_7/P_2)_P$	$\left(\frac{X_G}{C_G A_{10} P} \right)$ $\left(\frac{X_G}{C_G A_{10} P} \right)$
		7(b)	$\left(\frac{\frac{X_G}{C_G A_{10} P} + 1}{R_{o1}} \right)_P$	
22.	Turbine Disch. (stbd) P_{7S} (psi)	7(c)	$(P_7/P_2)_S$	
		7(d)	$\left(\frac{\frac{X_G}{C_G A_{10} P} + 1}{R_{o1}} \right)_S$	

E FLIGHT TESTS

FORMULAE OR CHARTS FOR I.B.M. 704 COMPUTER

SHEET NO. 10
 DATE: Sept. 1957

REPORT NO. 14-100-1-188
 PREP. BY: R. WAECHTER

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

$$P_1 = R_{o_1} p$$

$$\frac{\quad}{144}$$

$$\dot{W}_E = \frac{p_2 A_2 \sqrt{g}}{\sqrt{R T_2}} \left(\frac{p_2}{P_2} \right)^{\frac{\gamma-1}{\gamma}} \sqrt{\frac{2\gamma}{\gamma-1} \left[1 - \left(\frac{p_2}{P_2} \right)^{\frac{\gamma-1}{\gamma}} \right]}$$

Increase measured p_2 by 1% to allow for station of measurement

$$T_1 = T_{\text{amb}} (1 + .2 M^2)$$

$$P_1 = R_{o_1} p$$

$$\frac{\quad}{144}$$

Availability pending, can use ambient T_1 for computations

$\gamma = 1.4$
 $A_2 =$ effective engine face area initially $.97 \times \text{geom. area (sq. in.)}$
 $R = 96.02$ for T °K
 \dot{W}_E UNITS IN LBS/SEC

$$\left(\frac{X_G}{C_G A_{10} P} + 1 \right)_P = 3.06 \left(\frac{P_{7P}}{P} \right)^{.243} - 7.06 \text{ for } \frac{P_{7P}}{P} \leftarrow 1.852$$

$$= 1.255 \frac{P_{7P}}{P} \text{ for } \frac{P_{7P}}{P} \rightarrow 1.852$$

$$\left(\frac{X_G}{C_G A_{10} P} + 1 \right)_S = 3.06 \left(\frac{P_{7S}}{P} \right)^{.243} - 7.06 \text{ for } \frac{P_{7S}}{P} \leftarrow 1.852$$

$$= 1.255 \frac{P_{7S}}{P} \text{ for } \frac{P_{7S}}{P} \rightarrow 1.852$$

$P_{7/p}$ must be derived from consistent units

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 702

<u>INPUT</u>		<u>OUTPUT</u>		<u>APPL</u>
		β(a)	$\frac{X_{NP}}{p}$	$\frac{X_{NP}}{p}$
				$\frac{X_G}{p} =$
		β(b)	$\frac{X_{NS}}{p}$	Similar
				$A_{10} =$
				$=$
				$C_g = c$
				C
				$(m_E V$
23)	Turb. Disch. port T_{7P} °K	β(c)	T_{7P}/T_1	$\frac{T_{7P}}{T_1} =$
24)	Turb. Disch. stbd. T_{7S} °K	β(d)	T_{7S}/T_1	$\frac{T_{7S}}{T_1}$
25)	Port eng. fuel flow QP.E.	9(a)	$QP.E/P_1\sqrt{T_1}$	Input P_1 T_1

FLIGHT TESTS

FORMULAE OR CHARTS FOR I.B.M. 704 COMPUTER

11
Nov, 1957

71/PERF/2 ESS.2
R. Waechter

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

$$\frac{X_{NP}}{p} = \frac{X_{GP}}{p} - \frac{(m_E V)}{p}$$

$$\frac{X_G}{p} = \left[1.255 \frac{P_7}{p} - 1 \right] C_G A_{10} \text{ for } \frac{P_7}{p} \geq 1.352$$

Similar to 8 (a) output

$$A_{10} = \begin{cases} \text{constant for each engine initially } 508 \text{ "} \\ \text{A/B off} \\ = 924 \text{ " A/B on} \end{cases}$$

$$C_G = \begin{cases} \text{constant for all J75 engines} \\ \text{Chart III } C_G \text{ vs } \frac{P_7}{p} \text{ and } H_p, \text{ A/B off} \end{cases}$$

$$\text{Chart IV } C_G \text{ vs } \frac{P_1}{p}, \text{ A/B on}$$

$$(m_E V) = \frac{W_E M 65.3 \sqrt{T_0}}{32.2 \times p/144}$$

$$\frac{T_{7P}}{T_1} = \frac{T_{7P} \text{ } ^\circ\text{K}}{T_0 (1 + .2M^2)}$$

$$\frac{T_{7S}}{T_1} = \frac{T_{7S} \text{ } ^\circ\text{K}}{T_0 (1 + .2M^2)}$$

$$\frac{X_G}{p} = 3.06 \left[\left(\frac{P_7}{p} \right)^{.243} - 1 \right] C_G A_{10}$$

for $\frac{P_7}{p} < 1.352$

$\frac{P_7}{p}$ must be derived from consistent units

Require A/B on or off signal (or Q_{A/B} signal) to differentiate A₁₀ and C_G for A/B on and off

W_E in lbs/sec. (see output 6c and d)

Input Q = out.Q

$$P_1 = R_{O1} \times p \frac{\cdot}{\cdot} 144$$

$$T_1 = T_0 (1 + .2M^2)$$

ARCC I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.B.M. 704

	<u>INPUT</u>	<u>OUTPUT</u>	<u>APPLICA</u>
26)	Stbd. eng. fuel flow $Q_{S.E.}$	9(b) $Q_{S.E.} / P_1 \sqrt{T_1}$	
27)	Port A/B fuel flow $Q_{P.A.}$	9(c) $Q_{P.A.} / P_1 \sqrt{T_1}$	Input Q $P_1 =$
28)	Stbd. A/B fuel flow $Q_{S.A.}$	9(d) $Q_{S.A.} / P_1 \sqrt{T_1}$	$T_1 =$
29)	By-pass air T_B (port) above and below mid jet pipe No. 45 and 46 FAR/105/1 Part 3, Iss. 9.		Average convert
30)	By-pass air p_B (port) below mid jet pipe No. 61 of FAR/105/1 Part 3, Iss. 9.		Take mid
31)	By-pass air $p_B - p_i$ (port) where p_B is near final nozzle No. 63 FAR/105/1 Part 3, Iss. 9.		$(p_B -$
		10(a) W_B (port)	$W_B = P$ \sqrt{RT}
		10(b) F_N/p (port)	$F_N/p = F$ p
		10(c) F_N/p (stbd)	$mV/p =$
			$F_G =$ p $=$

LIGHT TESTS

FORMS OR CHARTS FOR I.B.M. 704 COMPUTER

REPORT NO. 12 REPORT NO. 71/PERF/2 Iss. 2
 DATE OCT, 1957 PREP. BY R. Waechter

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

Input Q = output Q
 $P_1 = R_{O1} P \cdot \frac{\cdot}{\cdot} 144$
 $T_1 = T_0 (1 + .2M^2)$

Average upper and lower readings
 & convert T_B from $^{\circ}F$ to $^{\circ}K$

Assume identical on stbd side

Take mid jet pipe $P_B \approx \frac{P_B \text{ near final nozzle}}{1.07}$

Assume identical on stbd side

i.e. mid jet pipe $M \approx .31$
 $(P_B - P_i) + \frac{P_i}{144} = P_B$

P_i = indicated ambient static

Assume P_B identical on stbd. side

$$W_B = \frac{P_B A_B \sqrt{g}}{\sqrt{RT_B} \left(\frac{P_B}{P_B} \right)^{\frac{\gamma-1}{\gamma}}} \sqrt{\frac{2\gamma}{\gamma-1} \left[1 - \left(\frac{P_B}{P_B} \right)^{\frac{\gamma-1}{\gamma}} \right]}$$

$\gamma = 1.4$

Assume identical on stbd side

A_B = effective by-pass area near final nozzle, sq. inches for P_B in psi. (initially $A_B = .93 \times \text{sq. area}$)
 $R = 96.02$ for $T^{\circ}K$
 W_B units in lbs/sec.

$$\frac{F_N}{p} = \frac{F_G}{p} - \frac{mV}{p} - \frac{D_S}{p}$$

Use port engine data for calculating F_N/p port, and stbd

engine data for calculating F_N/p stbd ;

except W_B (port) can be used to determine (F_N/p) port and stbd.

$$\frac{mV}{p} = \frac{(W_E + W_B) M \times 65.8 \sqrt{T_0}}{32.2 \times 144}$$

$$\frac{F_G}{p} = \frac{F_G}{XG} \times \frac{XG}{p} \quad (\text{A/B on})$$

$$= \frac{FG}{XIG} \times \frac{XIG}{p} \quad (\text{A/B off})$$

Require A/B on or off (Q) signal

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I, B, M.

<u>INPUT</u>	<u>OUTPUT</u>	<u>A</u>
	10(d) μ (port)	$\frac{X}{p}$ $\frac{F}{X_i}$ $\frac{F}{X_c}$ $\frac{P}{I}$ μ
	11(e) μ (stbd)	μ w_T $\sqrt{T_1}$ $\frac{A}{c}$ $\frac{D_s}{p}$

FLIGHT TESTS

FORM OR CHARTS FOR I.B.M. 704 COMPUTER

REPORT NO. 13 REPORT NO. 71/PERF/2 Iss. 2
 DATE OCT. 1957 PREP. BY R. Waechter

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

$$\frac{X_{iG}}{p} = \frac{X_{iG}}{X_G} \times \frac{X_G}{p}$$

$$\frac{X_{iG}}{X_C} \text{ from chart V using } P_{T7/p}$$

$$\frac{X_G}{p} \text{ from 8a) output calcs.}$$

$$\frac{FG}{X_{iG}} \text{ (A/B off) from chart VI knowing } \mu \text{ and } \frac{P_{10}}{p}$$

$$\frac{FG}{X_G} \text{ (A/B on) from chart VII knowing } \mu \text{ and } \frac{P_{10}}{p}$$

$$\frac{P_{10}}{p} = 99\% \frac{P_7}{p} \text{ (A/B off)}$$

$$= \frac{C_g}{.965} \left(\frac{P_7}{p} \right) - \left(\frac{C_g}{1.206} \right) + 0.8 \text{ (A/B on)}$$

$$\mu = \frac{W_B}{W_E} \times \sqrt{\frac{T_B}{T_7}} \text{ (A/B off)}$$

Assumed

$\frac{P_7}{p}$ must be derived from consistant units

W_E assumed = W_{10} (A/B off)
 i.e. eng. fuel offsets airbleed and leakage

$$\mu = \frac{W_B}{W_{10}} \times \sqrt{\frac{T_B}{T_{10}}} \text{ (A/B on)}$$

$$W_{10} \approx W_E + \frac{Q_{A/B}}{3600} \text{ (A/B on)}$$

$$\sqrt{\frac{T_{10}}{A/B \text{ on}}} = \left[\frac{X_G \times .745}{W_E + \frac{Q_{A/B}}{3600}} \right] \times \left[\frac{.0009 \frac{X_G}{p} + 0.8}{.00219 \frac{X_G}{p} - .02} \right] \text{ } ^\circ K$$

$\frac{X_G}{p}$ (sq. inches) from 8(a) output calcs.

$$\frac{D_s}{p} = 4130 C_{D_s} M^2$$

$S = 40.98 \text{ sq. ft.}$
 $= 5,900 \text{ sq. inches}$

ARROW I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAE OR CHARTS FOR I.E.M. 704 COMB

INPUT		OUTPUT		APPLICABLE
				$C_{DS} = \frac{\partial C_{DS}}{\partial \left(\frac{m}{m_0}\right)}$ $\frac{\partial C_{DS}}{\partial \left(\frac{m}{m_0}\right)}$ from $\frac{P_{T_1}}{P_1}$ from a_1 in 'g' $D/P = \left(\frac{F_N}{P}\right)$ $\frac{(R)}{3}$ $($
		11(b)	3945 gL M $\sqrt{T_0}$	
		11(c)	D/P (at mean interval)	
		11(d)	C _D (at mean interval)	C _D = D/P
		12(a)	$\frac{V \delta}{Q}$	V = 38.9 M
		12(b)	$\frac{Q}{F_{NT} \sqrt{\theta}}$	Q = QP.E. F _{NT} = F _{NP} θ = T ₀ /
		12(c)	$\frac{Q_P}{X_{NP} \sqrt{\theta}}$	Q _P = Q _P .E
		12(d)	$\frac{Q_S}{X_{NS} \sqrt{\theta}}$	Q _S = Q _S .E

T TESTS

Iss. 2

CHARTS FOR I.E.M. 704 COMPUTER

1/
DATE Oct, 1957

REPORT NO. 71/PERF/2
PREP BY R. Waechter

APPLICABLE FORMULAE, OPERATION OR CHART

REMARKS

$$C_{DS} = \frac{\delta C_{DS}}{\delta \left(\frac{M_1}{M_0} \right)} \left[\frac{W_E + W_B + 5}{6.97 \frac{PM}{\sqrt{T_0}}} - \frac{.308(1+.2M^2)^3}{M} \left(\frac{P_{th}}{P_1} \right) \right]$$

Spillage drag coefficient
See Report 70/PERF/1 App.II
for derivation

$$\frac{\delta C_{DB}}{\delta \left(\frac{M_1}{M_0} \right)} \text{ from Chart VIII}$$

$$\frac{P_{th}}{P_1} \text{ from Chart IX}$$

a_L in 'g' units

For comparison with $(R/C)_2$

$$D/P = \left(\frac{F_{NP}}{P} + \frac{F_{NS}}{P} \right) \cos(\alpha - 2.58^\circ) \text{ at mean interval}$$

In steady level flight
 $D/p = \left(\frac{F_{NP}}{P} + \frac{F_{NS}}{P} \right) \cos(\alpha - 2.58^\circ)$
not at mean interval.

$$\frac{(R/C)_1}{3945 M \sqrt{T_0}} \times \frac{W}{P}$$

May substitute $\left(a_L \times \frac{W}{P} \right)$ by $\left(\frac{(R/C)_2}{3945 M \sqrt{T_0}} \times \frac{W}{P} \right)$

$$(a_L \times \frac{W}{P}) \text{ at mean interval}$$

if $(R/C)_2$ has less scatter than
 $(3945 a_L M \sqrt{T_0})$.

$$C_D = D/p \times \frac{1}{123,600 M^2}$$

In steady level flight C_D does
not occur at mean interval

$$V = 38.9 M \sqrt{T_0} \text{ (knots)} \quad \delta = 1/2116$$

Steady level flight only

$$Q = Q_{P.E.} + Q_{S.E.} + Q_{P.A.} + Q_{S.A.}$$

$$F_{NF} = F_{NP} + F_{NS}$$

$$\Theta = T_0/288$$

$$Q_P = Q_{P.E.} + Q_{P.A.}$$

$$Q_S = Q_{S.E.} + Q_{S.A.}$$

ANNEX I - PERFORMANCE FLIGHT TESTS

INPUT - OUTPUT SUMMARY AND APPLICABLE FORMULAS OR CHARTS FOR I.E.S. 704

<u>INPUT</u>	<u>OUTPUT</u>	<u>APPLI</u>
	13(a) $\frac{L}{P}$ 13(b) C_L 13(c) C_L^2 13(d) M_B (port only)	$\frac{L}{P} =$ $C_L =$ $M_3 =$
	14(a) M_2 (port) 14(b) M_2 (stbd) 14(c) R (N.A.M)	$M_{2P} =$ Similar $R = \sum$

	APPLICABLE FORMULAE, OPERATION OR CHART	REMARKS
y)	$\frac{L}{P} = \frac{W_0 + \sum F}{P/144} - \left(\frac{F_N}{P} \text{ port + stbd.} \right) \sin(\alpha - 2.58^\circ)$ $C_L = \frac{L/p}{\frac{\gamma}{2} M^2 S} \quad \text{where } \gamma = 1.4$ $S = 176,300 \text{ sq. inches}$ $M_3 = \sqrt{5 \left[\left(\frac{P_B}{P} \right)^{0.286} - 1 \right]}$	<p>where 2.58° = angle of thrust axis relative to fuselage datum</p> <p>Note:- P_B (near exit.) \approx measured mid jet pipe $P_B \times 1.07$</p>
	$M_{2p} = \sqrt{5 \left[\left(\frac{P_2}{P} \right)^{0.286} - 1 \right]}$ <p>Similar to 14a)</p> $R = \sum (38.95 M \sqrt{T_0} \times \Delta T_{HRS})$	<p>Increase measured P_2 by 1% to allow for station of measurement</p>



AVRO AIRCRAFT LIMITED
MALTON, ONTARIO

TECHNICAL DEPARTMENT

REPORT NO. 71/PERF/2 Iss.2

SHEET NO. _____

AIRCRAFT:

ARROW 1

PERFORMANCE FLIGHT
TESTS

PREPARED BY

DATE

R. Waechter

Nov. 1957

CHECKED BY

DATE

Chart I (nose probe pitot correction) of

$$\Delta \left(\frac{P_{Ti}}{P_i} \right) \text{ versus } \frac{P_{Ti}}{P_i} \text{ where } \frac{P_{Ti}}{P_i} + \Delta \left(\frac{P_{Ti}}{P_i} \right) = \frac{P_T}{P_i}$$

will be inserted when flight results become available.

Initially $\Delta \left(\frac{P_{Ti}}{P_i} \right)$ is assumed zero, until flight results prove otherwise.

Chart I



AVRO AIRCRAFT LIMITED
MALTON - ONTARIO

TECHNICAL DEPARTMENT

REPORT NO. 71/PERF/2 APP.I

SHEET NO. 1

AIRCRAFT:

ARROW I

PERFORMANCE
FLIGHT TESTS

PREPARED BY

DATE

R. Waechter

Nov. 1957

CHECKED BY

DATE

AIRCRAFT WEIGHT AND C.G. DATA (For reference only, see also report No. 7-0400-44-10)

First aircraft, operational weight empty O.W.E., no ballast = 47,759 lb.

with C.G. at sta. 554.51" = 32.7% M.A.C.

Standard MK I, O.W.E. with 959 lb. ballast at sta. 86.60" = 48,718 lb.

with C.G. at sta. 545.30" = 30.2% M.A.C.

MK I first flight, O.W.E. with 1432 lb. at sta. 89.16" and 165 lb. in Nav. seat = 49,356 lb. with C.G. at sta. 541.8" = 29.2% M.A.C.

The above C.G. positions and A/C weights are given for the normal "in flight" condition with ^u/c up and water methonal and alcohol tanks full, and with cylindrical ejector. On later flights a divergent ejector will be fitted, increasing the A/C weight by 204 lbs. including 79 lbs. ballast to maintain C.G. at the same position. All C.G. and A/C weight values, should be checked by actual weighings before flight and after any A/C modifications.

Correction for ^u/c down and water methonal and alcohol tanks empty = + 0.8%. Using fuel system proportioners, aft C.G. limits therefore are
31% M.A.C. for Standard MK I
30% M.A.C. for MK I first flight.

Effect of ^u/c position is such that the C.G. is shifted aft by .55% M.A.C. at 43,500 lb. A.U.W. and .39% M.A.C. at 68,561 lb. when the ^u/c is selected down.

Draining of the water methonal and alcohol tanks causes a mean aft C.G. shift of approx. 0.22% M.A.C. These tanks should always be full or ballasted unless specifically mentioned in the flight report after each flight.

For the standard MK I airplane, with ^u/c up and water methonal and alcohol tanks full, and using fuel system proportioners the aircraft C.G. position varies linearly from 29.68% M.A.C. at 68,561 lb. A.U.W. (full fuel) to 30.20% M.A.C. at 48,718 lb. A.U.W. (no useable fuel). This total variation is only 0.52% M.A.C. with a rate of change of + .026% per 1000 lb. decreased A.U.W. Hence C.G. position could readily be estimated "by hand" at any stage of flight knowing:-

- 1) Initial C.G. position, (C.G.)₀
- 2) Total fuel used in a given flight, F (lbs)
- 3) Flight time to point under consideration ΔT and
- 4) Total flight time, T

$$\text{i.e. C.G. position} = (\text{C.G.})_0 + \frac{\Delta T}{T} \times \frac{F}{1000} \times .026$$



AVRO AIRCRAFT LIMITED
MALTON - ONTARIO

TECHNICAL DEPARTMENT

REPORT NO. 11/PERF/2 APP. I

SHEET NO. 2

AIRCRAFT:

ARROW I

PERFORMANCE FLIGHT
TESTS

PREPARED BY

DATE

R. Waechter

Nov. 1957

CHECKED BY

DATE

This value can be used to check an "IBM 704 computed" value based on fuel remaining measurements from 14 fuel tanks. This latter method is more universal in determining C.G. position for any possible variations in fuel sequencing but depends on the reliability of 14 fuel tank measurements. The following table gives the useable fuel capacities and horizontal C.G. positions of the 14 fuel tanks.

Tank	Useable Fuel Capacity at 7.8 lbs. per gallon	C.G. Position	
		Station	%M.A.C.
1. (fuselage)	2161 lbs.	354.35"	-22.5
2. (fuselage)	2192 "	433.99"	- 0.5
3. (port + stbd. wing)	2355 "	446.14"	2.8
4. " " "	1404 "	502.47"	18.4
5. " " "	2278 " (collector)	548.87"	31.2
6. " " "	2402 "	589.11"	42.3
7. " " "	4352 "	627.57"	52.8
8. " " "	2699 "	675.52"	66.0
	<u>19,843 lbs.Total</u>		



AVRO AIRCRAFT LIMITED
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REPORT No. 71, Part 2 App. 1

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AIRCRAFT: ARROW I	PERFORMANCE FLIGHT TESTS	PREPARED BY	DATE
		R. Waechter	Nov. 1957
		CHECKED BY	DATE

Note % M.A.C. = $\frac{\text{C.G. sta.} - 435.82''}{362.61''} \times 100$

Hence for I.B.M. 704 computations, the aircraft C.G. position is determined as follows:-

- a) Denote fuel remaining in fuelage tanks as F_1 & F_2
- b) Add port & etbd wing fuel from corresponding tanks and denote F_3, F_4, F_5, F_6, F_7 & F_8 .
- c) Denote O.W.E. = W_0 and initial C.G. @ $W_0 = (C.G.)_0$ for U/C up and water methonal and alcohol tanks full. Then at any time during flight with U/C up:- C.G. % M.A.C. =
$$\frac{W_0 \times (C.G.)_0 - 22.5F_1 - 0.5F_2 + 2.8F_3 + 18.4F_4 + 31.2F_5 + 42.3F_6 + 52.8F_7 + 66.0F_8}{W_0 + \sum F}$$

If the aircraft is weighed prior to flight with full fuel, and C.G. determined by relative weights on main & nose wheele, then $(C.G.)_0$ for U/C up = $(C.G. \text{ as meas. U/C down}) \times (W \text{ as meas.}) - 28.4 \times 19,843 - .55 \times 48,500$

$(W \text{ as meas.}) - 19,843$

Where 28.4 = fuel C.G. position (% M.A.C.) tanks full or porportionately full
19,843 = useable fuel tank fuel when full (lbe)
.55 = A/C C.G. ehift, % M.A.C., when the U/C is selected up @ $W = 48,500 \#$

16

14

11



AVRO AIRCRAFT LIMITED
MALTON, ONTARIO

TECHNICAL DEPARTMENT

REPORT No. 71/PERF/2 App. I

SHEET No. 4

AIRCRAFT:

ARROW I

PERFORMANCE FLIGHT
TESTS

PREPARED BY

DATE

R. Waechter

Nov. 1957

CHECKED BY

DATE

ACCURACY REQUIRED IN C.G. MEASUREMENT

1. At 50,000 feet $C_M = 1.5$ to $1.5g$, 1° change in elevator angle change aircraft drag approximately 4% (ref:- 72/PERF/4).
2. At 50,000 feet $C_M = 0.9$ to 2.0 lg , a shift of 2% MAC in C.G. position will change the required elevator angle for trimmed flight by 1° ($\pm 0.2^\circ$)
3. 1° elevator change per 2% MAC shift in C.G. position at 50,000 feet at $M = 0.9$ to 2.0 lg is directly proportional to g loading and will approximately double its value at 60,000 feet.
4. Using 50,000 feet $C_M = 1.5$ to $1.5g$ as design criteria, then 1.0° elevator change $\approx 1.33\%$ MAC shift in C.G. position $\approx 4.0\%$ Change in A/C drag.

Therefore, for 1% error in drag, elevator angle must be measured to within $\pm \frac{1}{4}$ or $\pm 0.25^\circ$ and c.g. position must be measured to within $\pm 1.33/4$ or $\pm 0.33\%$ M.A.C. Since the total C.G. travel is only .52% M.A.C. (using fuel system proportioners) a complete flight from full fuel to no fuel need only be broken into 2 stages of constant mean C.G. position.

CF 105

REV. 2/WT/121

ESTIMATED POSITION ERROR CORRECTION
FOR NOSE PROBE ~ STATIC

$$\frac{P_T}{P} = \frac{P_s}{P_L} + \Delta \left(\frac{P_T}{P_L} \right)$$

P_T = TRIM INDICATED TOTAL PRESSURE

P_L = INDICATED STATIC PRESSURE

P = TRIM AMBIENT STATIC PRESSURE

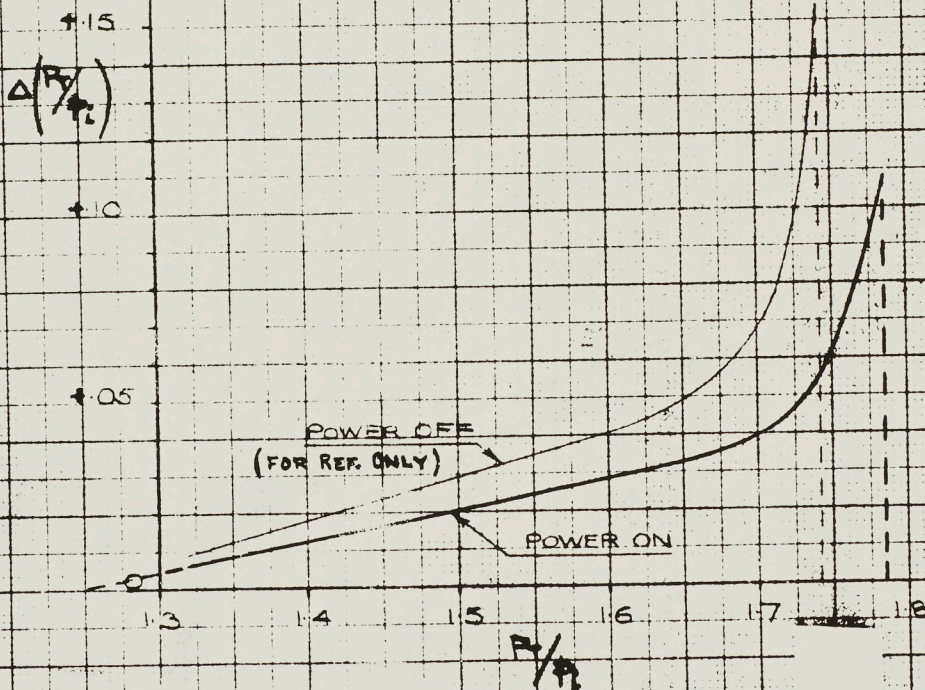


CHART II

16

14

10

CONFIDENTIAL

PRATT & WHITNEY AIRCRAFT

JT4A-20, -23 & -26 TURBOJET ENGINES

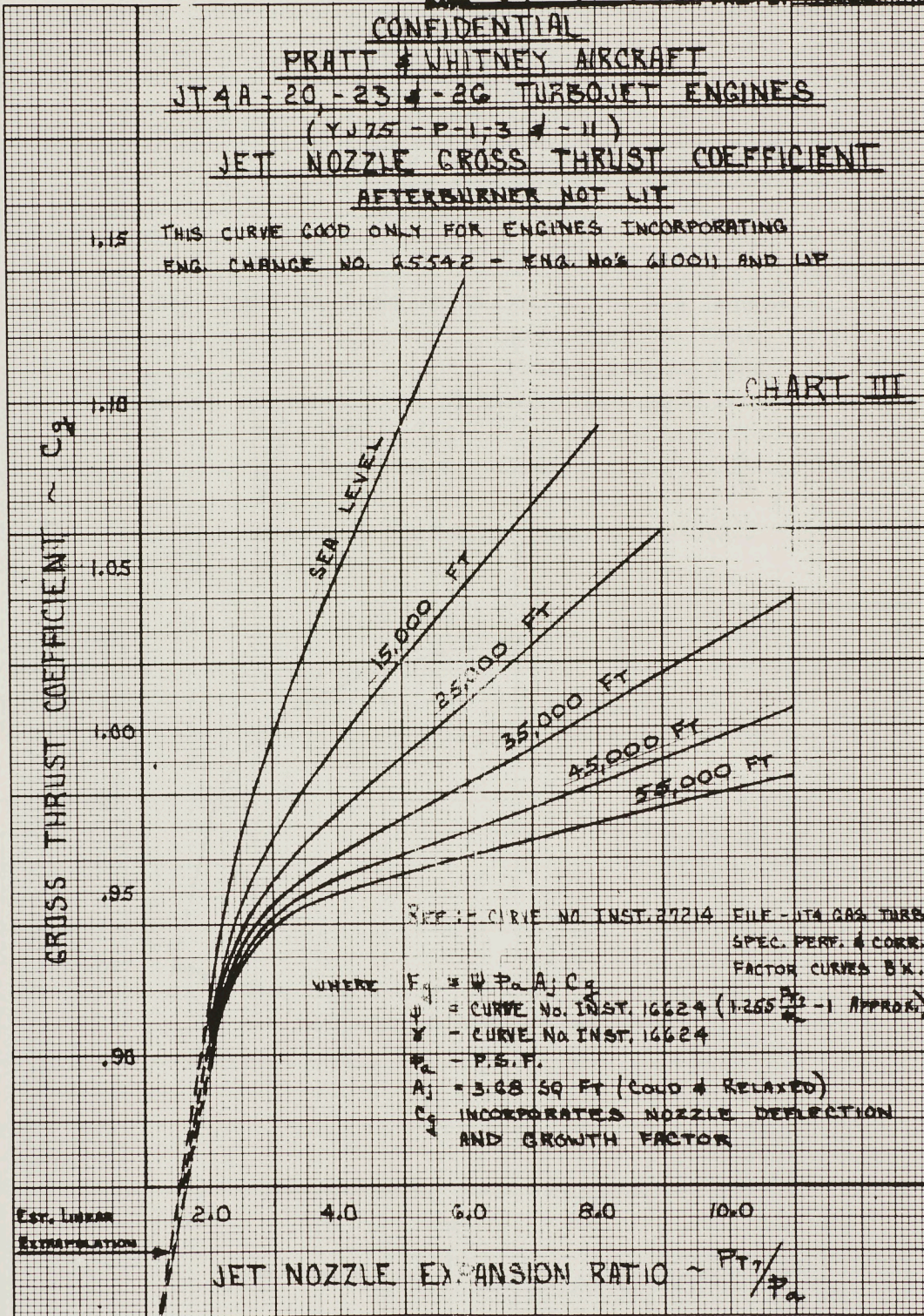
(YJ75-P-1, 3 & -11)

JET NOZZLE GROSS THRUST COEFFICIENT

AFTERBURNER NOT LIT

THIS CURVE GOOD ONLY FOR ENGINES INCORPORATING
 ENG. CHANGE NO. 65542 - ENG. NO. 61001 AND UP

CHART III



REF: CURVE NO INST. 27214 FILE - JTA GAS TURB. SPEC. PERFORM. & CORR. FACTOR CURVES B.K.

WHERE $F_g = \psi P_a A_j C_g$
 ψ = CURVE NO. INST. 16624 (1.285 $\frac{P_t}{P_a} - 1$ APPROX.)
 ψ = CURVE NO. INST. 16624
 P_a = P.S.F.
 A_j = 3.68 SQ FT (COLD & RELAXED)
 C_g INCORPORATES NOZZLE DEFLECTION AND GROWTH FACTOR

SHEET NO.

REPORT NO. 74/PB02

DATE 3/9/57

PREP BY R. W. RECHTER

CONFIDENTIAL
PRATT & WHITNEY AIRCRAFT
JT4A-20, -23 & -26 TURBOJET ENGINES
(YJ75-P-1, -3 & -11)
JET NOZZLE GROSS THRUST COEFFICIENT
AFTERSURNER LIT

REF: CURVE NO. INST. 1B151 FILE - JT4 GAS TURBINE
 SPEC. PERFORM. AND CORR.
 FACTOR CURVES BOOK

BASED ON MODEL TEST & ENGINE PERFORMANCE DATA

$$F_d = \psi P_a A_j C_d$$

ψ - FROM CURVE NO. INST. 14629 ($1.255 \frac{P_{T2}}{P_a}$) APPROX.

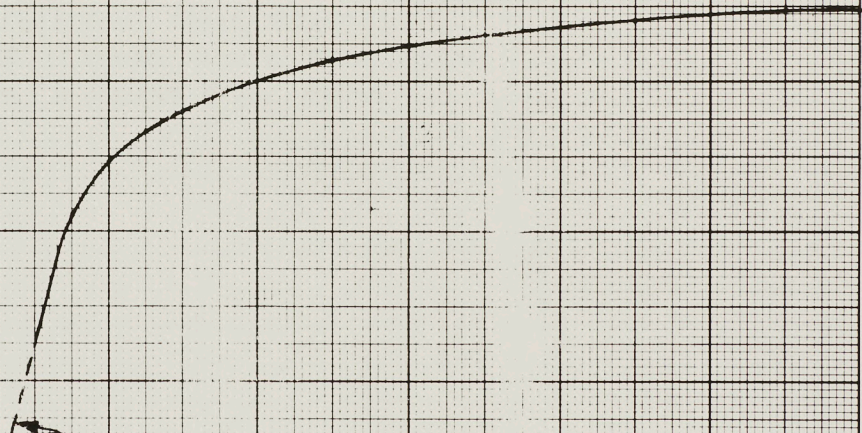
P_a - P.S.F.

$A_j = 6.398$ SQ. FT (EST. OPERATING)

$\gamma = 1.30$

GROSS THRUST COEFFICIENT - C_d

.90
 .85
 .80
 .75
 .70



THIS PORTION OF CURVE IS CALCULATED
 AND NOT YET CONFIRMED BY TEST

CHART IV

2.0 4.0 6.0 8.0 10.0 12.0

JET NOZZLE EXPANSION RATIO - $\frac{P_{T2}}{P_a}$

16

14

IDEAL GROSS THRUST RATIO

VS

PRIMARY PRESSURE RATIO

$$\frac{X_{Ic}}{X_c} = \frac{1.9 \frac{P_{10}}{\bar{p}} \sqrt{1 - \frac{10}{\gamma} \frac{P_{10}}{P_{10}}}}{0.255 \frac{P_{10}}{\bar{p}}}$$

FOR $\gamma = 1.33$

- X_{Ic} = IDEAL GROSS THRUST
 - X_c = TRUE GROSS THRUST
 - P_{10} = PRIMARY NOZZLE TOTAL PRESS.
 - \bar{p} = AMBIENT STATIC PRESS.
- } PRIMARY

$\frac{X_{Ic}}{X_c}$

1.10
1.08
1.06
1.04
1.02
1.00

PRIMARY PRESSURE RATIO

$\frac{P_{10}}{\bar{p}}$

CHART V

(TO BE USED FOR 175 $\frac{1}{8}$ OR CASE ONLY)

0 2 4 6 8 10 12

DIVERGENT EJECTOR

$$\frac{D_2}{D_1} = 1.70$$

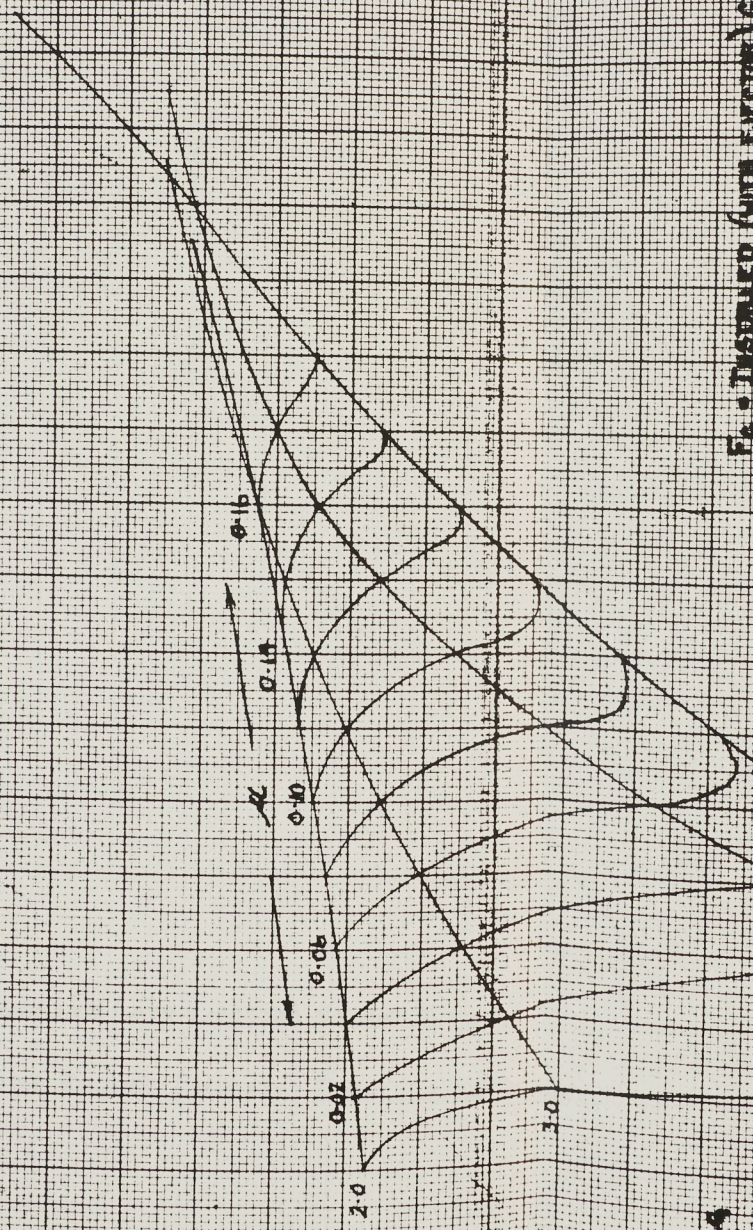
$$\frac{D_3}{D_2} = 1.34$$

$$\frac{L}{D_2} = 1.07$$

$$\theta = 9^\circ 25'$$

NACA SOLUTION $\frac{1}{D_2}$ OFF

REF. ρ/ρ_{02} OR FIG. 6(a-f)



F_2 - DISRUPTED (WITH EJECTOR) CROSS-THROAT

F_2/X_2

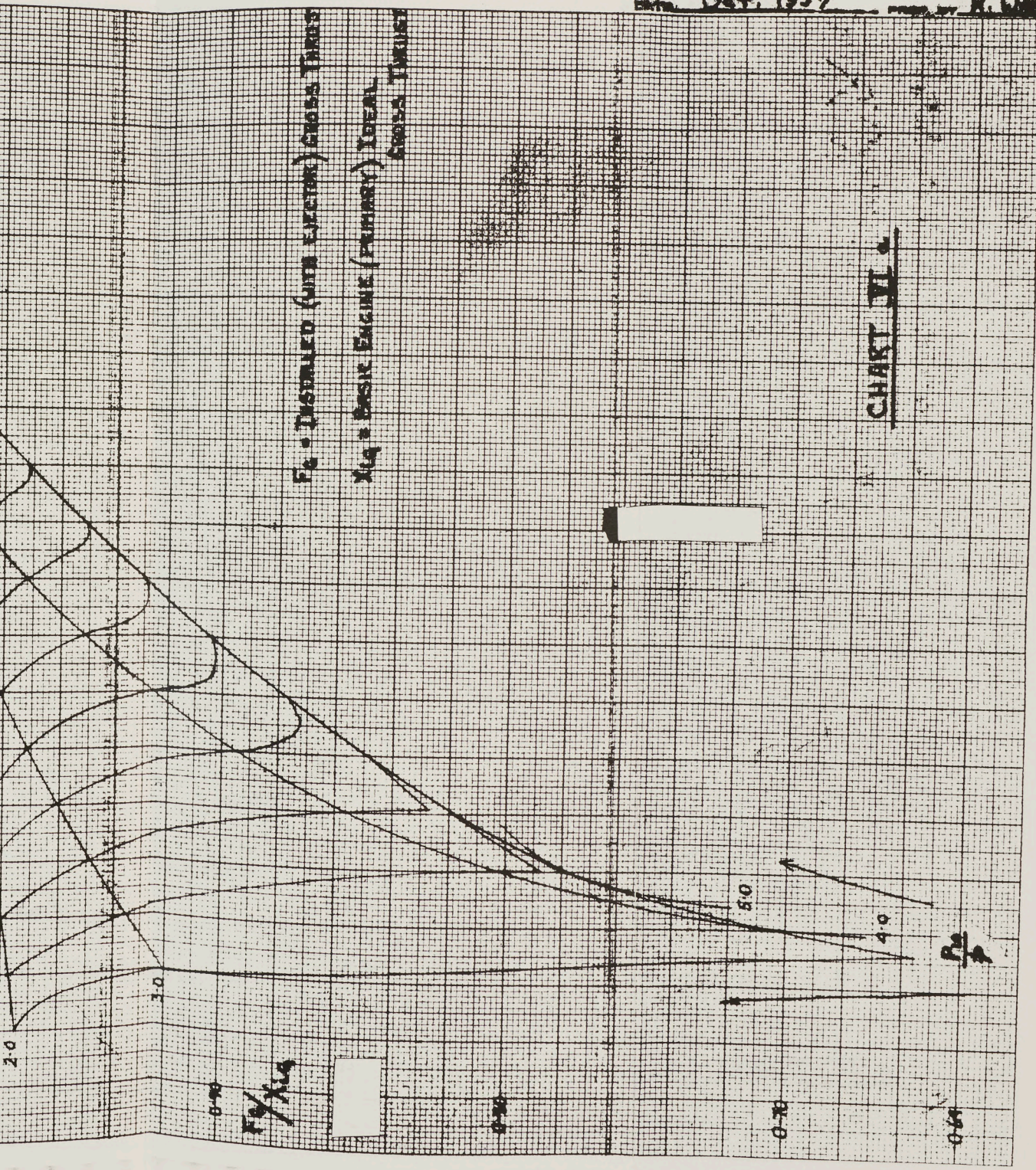
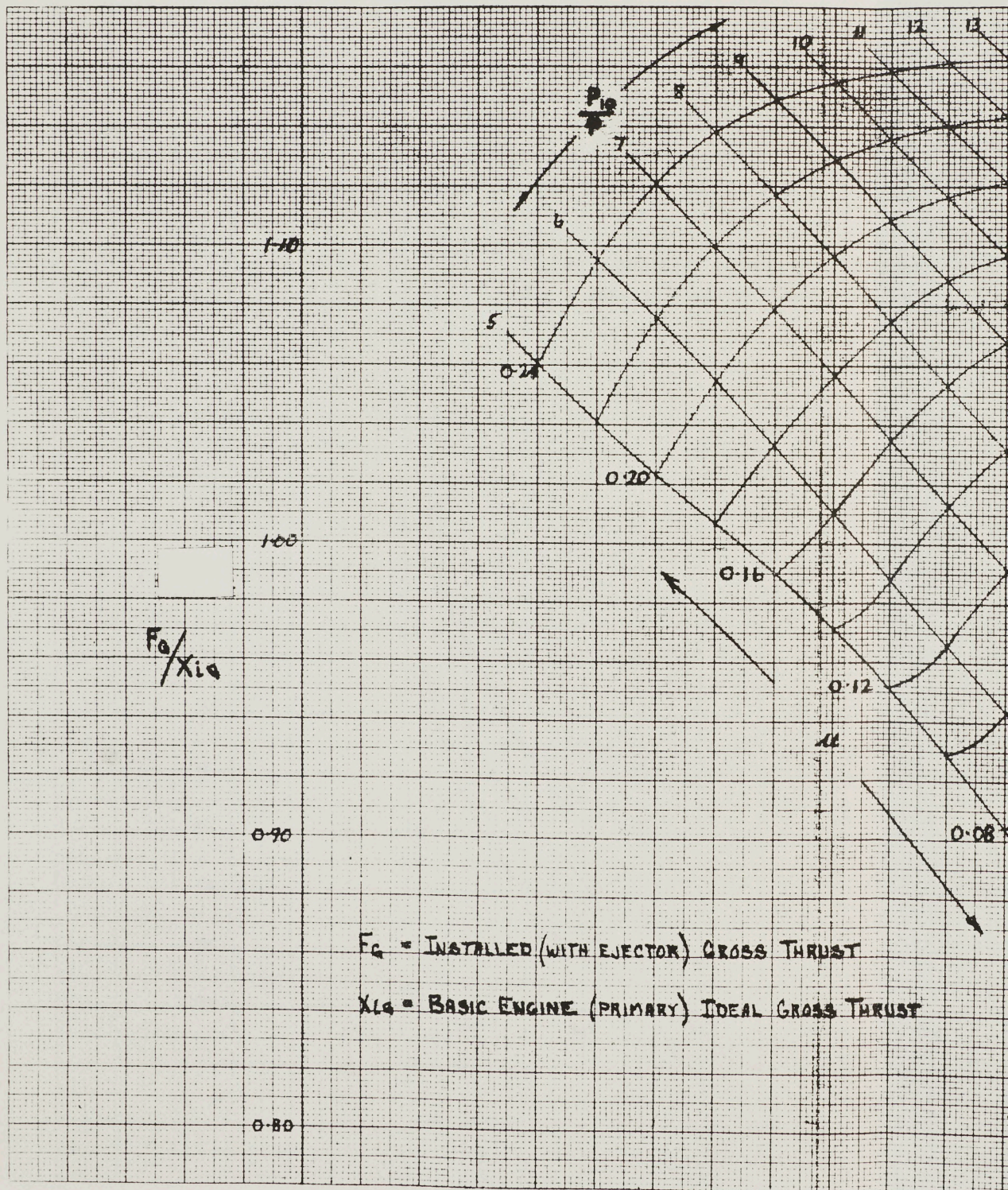
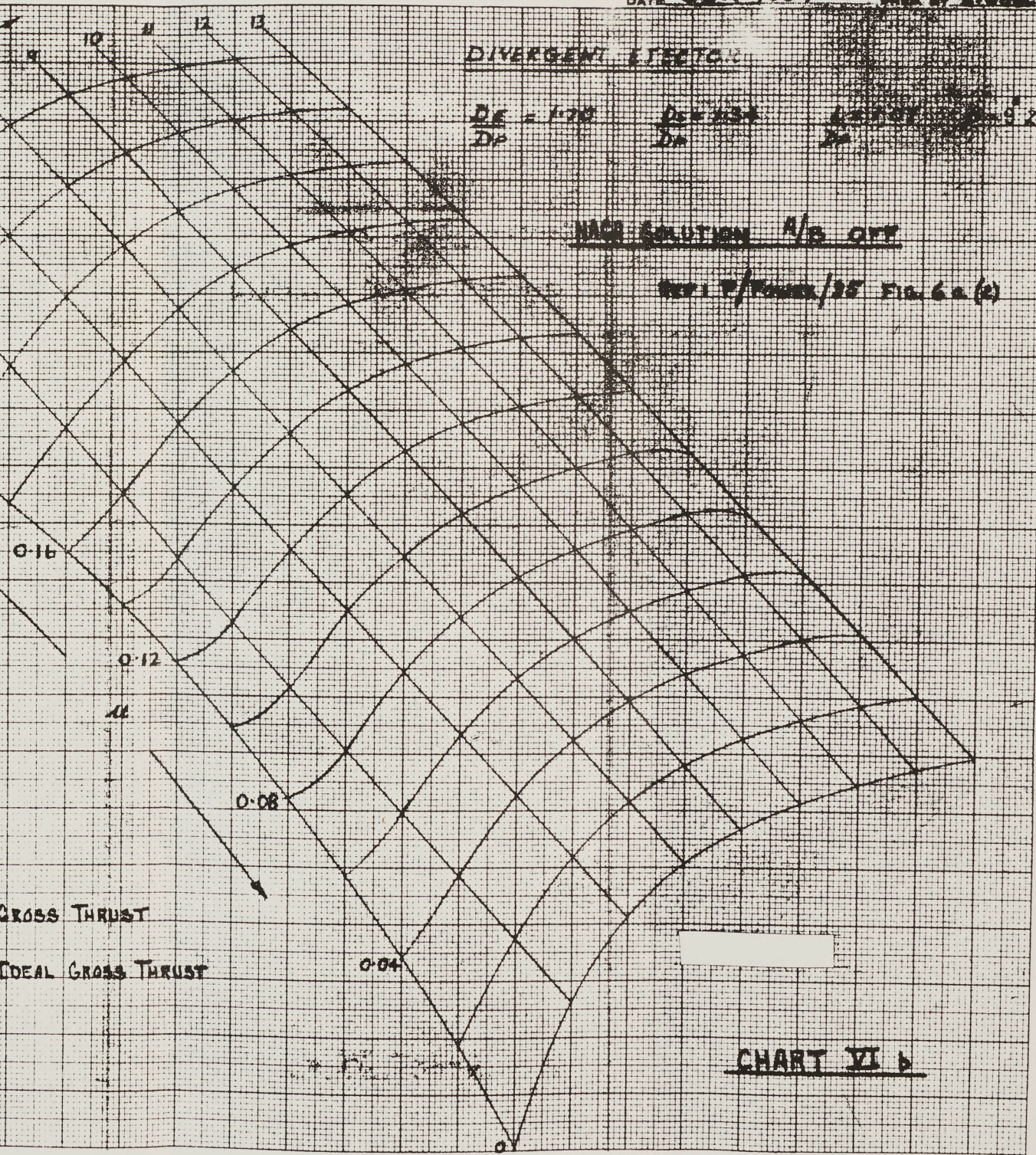


CHART VI





AVRO-NOBEL TEST RESULTS FOR J-7

AFTERBURNER ON

$D_e/D_n = 1.34$

$D_e/D_p = 1.07$

F_G = INSTALLED (WITH EJECTOR) GROSS THRU

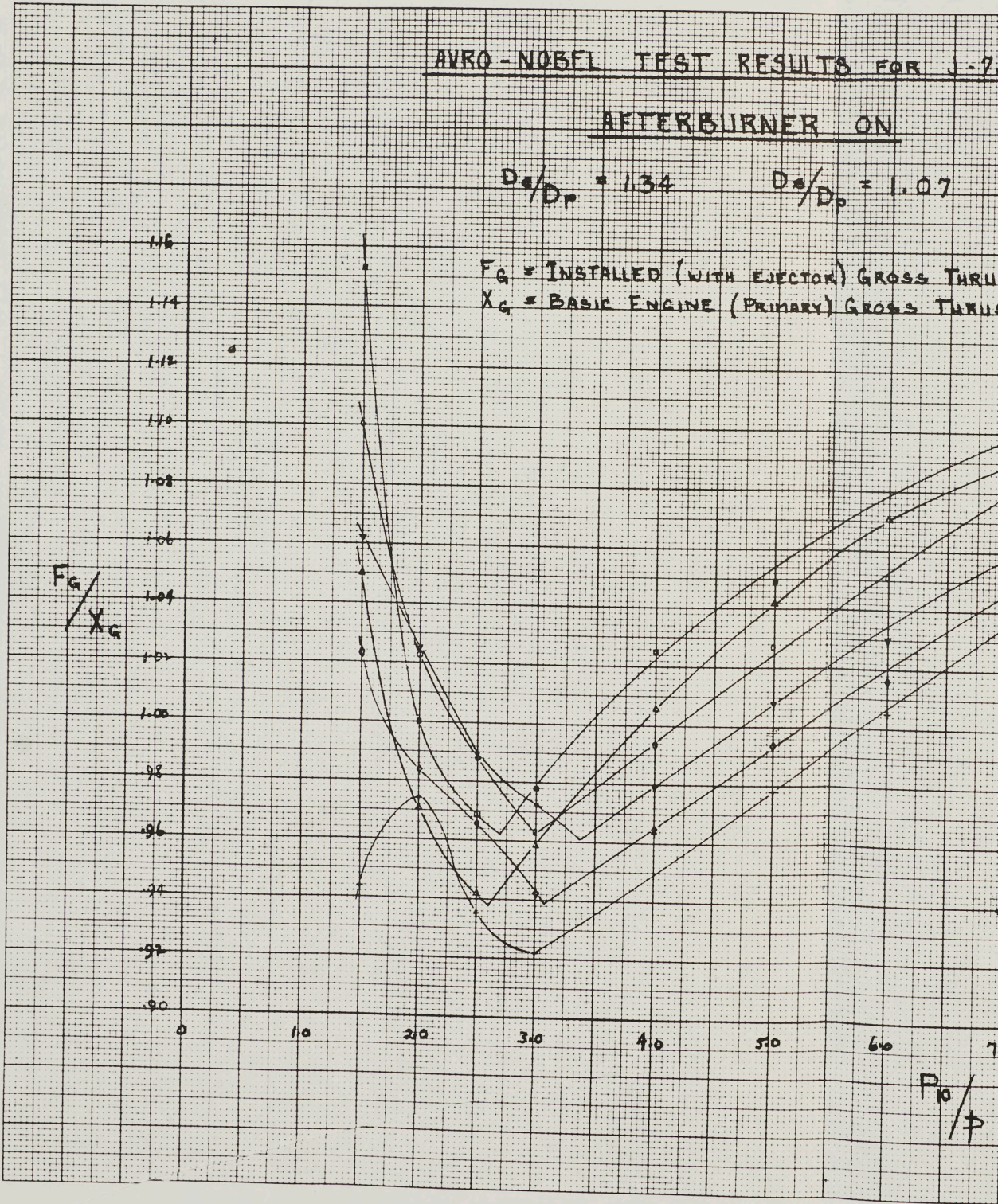
X_G = BASIC ENGINE (PRIMARY) GROSS THRU

F_G/X_G

1.16
1.14
1.12
1.10
1.08
1.06
1.04
1.02
1.00
0.98
0.96
0.94
0.92
0.90

0 10 20 30 40 50 60 70

P_0/P



TEST NO.

REPORT NO. 71/PERF/2 ISS.2

DATE

Nov. 1957

PREP. BY R. WAGHTER

TEST RESULTS FOR J-75 DIVERGENT EJECTOR

COMBURNER ON

$D_s/D_o = 1.07$

REF. 71/INT. AERO/1

(WITH EJECTOR) GROSS THRUST
LINE (PRIMARY) GROSS THRUST

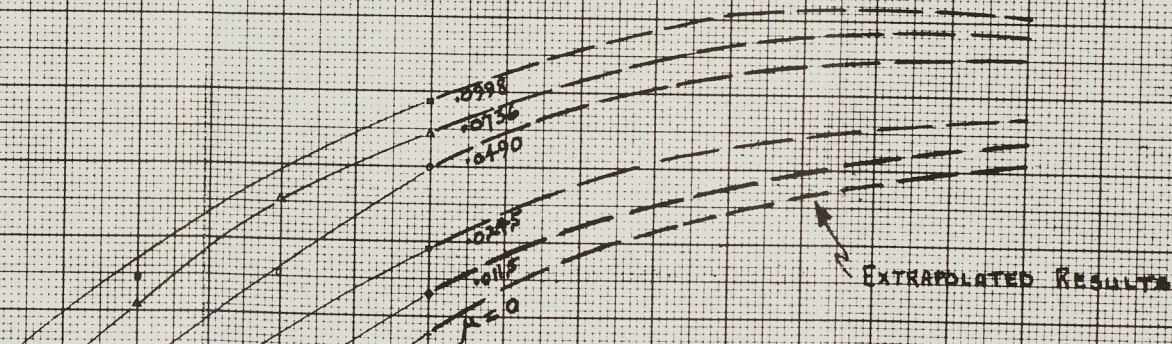


CHART VII

5.0 6.0 7.0 8.0 9.0 10.0 11.0

P_0/P

FORM NO.

DEC. 1957

REPORT NO.

71/PERF/2 ISS. 2

John Carter

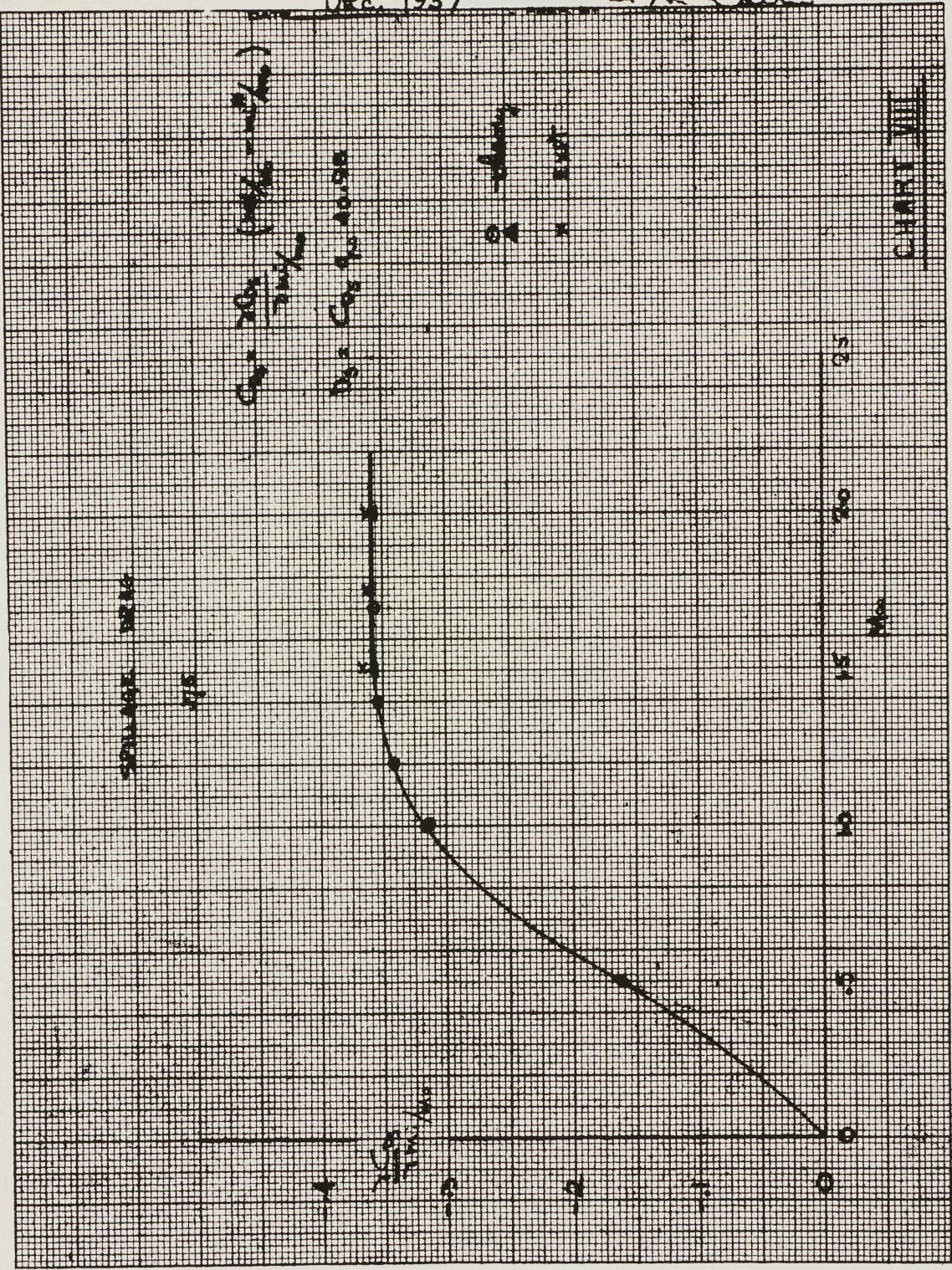


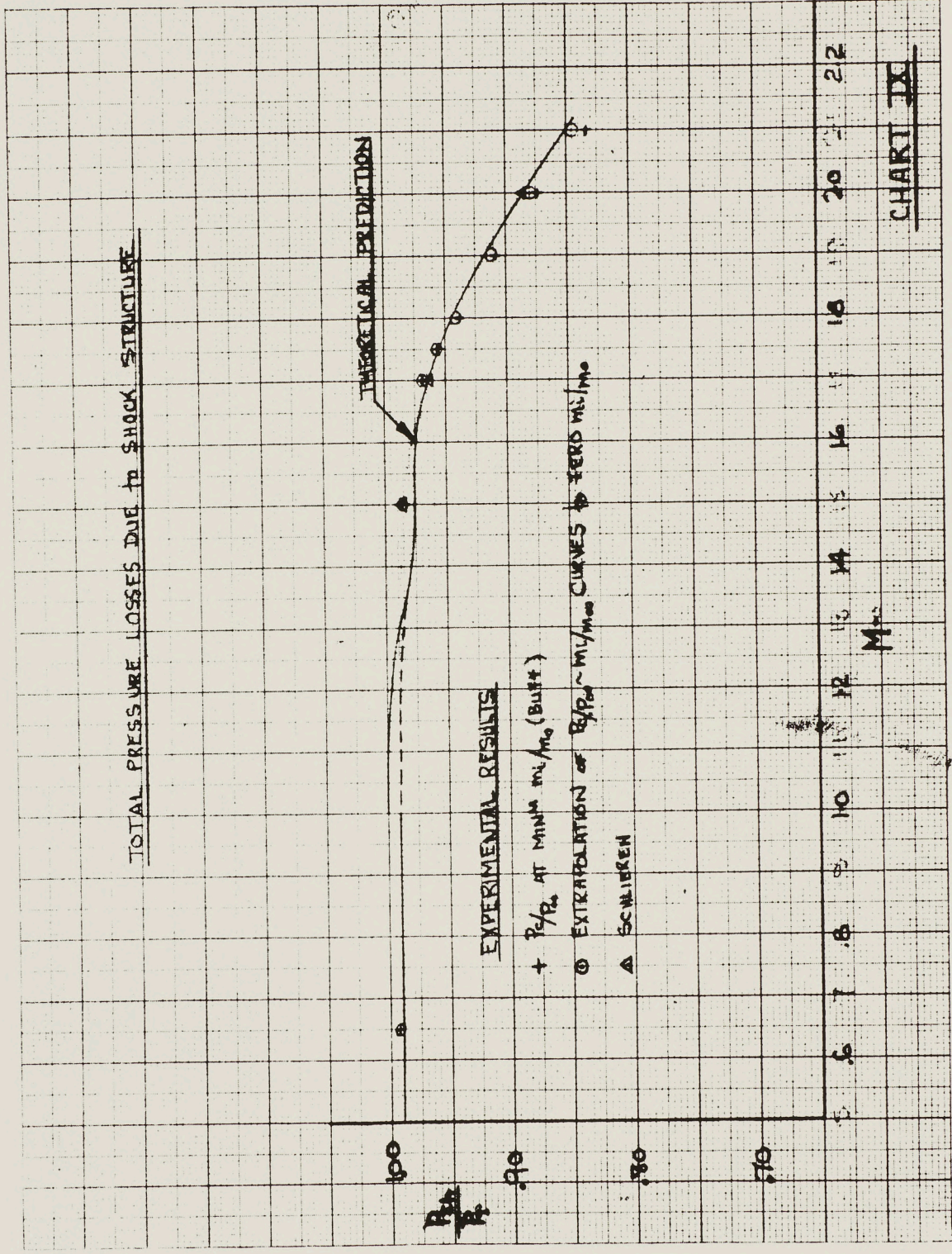
CHART VIII

16

14

13

TOTAL PRESSURE LOSSES DUE TO SHOCK STRUCTURE



THEORETICAL PREDICTION

EXPERIMENTAL RESULTS

- + P_{02}/P_{01} AT MIN M_2/M_0 (BUFF)
- EXTRAPOLATION OF $P_{02}/P_{01} \sim M_2/M_0$ CURVES TO ZERO M_2/M_0
- △ SCHLIEREN

CHART IX