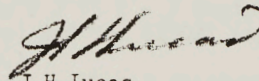


AVRO AIRCRAFT LIMITED

INTER-DEPARTMENTAL MEMORANDUM

Ref: 3272/04/J  
Date: October, 1957  
To: Mr.J.D.Hodge - Technical Flight Test Co-ordinator  
From: J.H.Lucas - Chief of Performance Evaluation  
Subject: ENGINE THRUST FROM ARROW 1 FLIGHT TESTS

Attached herewith, please find Appendix II to report 70/PERF/1 on Measurement of Engine Thrust from Arrow 1 Flight Tests. This appendix deals with adequacy of available instrumentation, applicable formulae and test bed calibration results.



J.H.Lucas  
Chief of Performance Evaluation

c.c Messrs: J.A.Chamberlin  
F.H.Brame  
D.N.Scard  
D.R.Woolley  
G.Esilman

Central Files - without encl.



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TECHNICAL DEPARTMENT

REPORT NO. 70/PERF/1 APP II

SHEET NO. 1

AIRCRAFT:

ARROW I

ENGINE PERFORMANCE

PREPARED BY

DATE

R. Waechter

Oct. 1957

CHECKED BY

DATE

MEASUREMENT OF Y J 75 ENGINE THRUST DURING ARROW I FLIGHT TESTS

1) SUMMARY

This appendix to report 70/Perf/1 summarizes a thrust measurement technique to be used during Arrow I flight tests. Use is made of available instrumentation only; therefore adequacy of instrumentation is discussed. Applicable formulae are given, to be used in conjunction with report 71/Perf/2 on Programming for Performance Data from Arrow I Flight Tests.

Results of Pratt and Whitney Aircraft Run-in and Final Acceptance Engine test bed calibration runs are also contained herein from which the following information is extracted for Y J 75 P - 3 Engines No. 610034 (port), No. 610029 (stbd), No. 610026 (spare) and No. 610027 (spare) for Arrow I Aircraft No. 1

Military thrust rating = 15,500 lbs. static sea level standard thrust with corresponding H.P. Comp. R.P.M.'s of 3630, 3690, 3690 & 3715 respectively. Each of these rpms are increased between 10 and 35 rpm to obtain N<sub>2</sub> Data Plate speeds of 98.80, 99.55, 99.72 and 99.72% respectively based on 3750 as 100% rpm. (see note 1).

Average L.P. Comp. R.P.M. at military thrust = 0.768 N<sub>2</sub> for existing engines

Average "Aerodynamic " nozzle area = 510 ( $\pm$  2) sq. inches (A/B off) 923, 921, 947 and 917 sq. inches (A/B on).

These aerodynamic nozzle areas should be used in conjunction with the gross thrust coefficient curves of report 71/Perf/2 Charts III and IV to determine effective nozzle area.

NOTE:- 1) Pratt and Whitney Aircraft have stated that 100% N<sub>2</sub> R.P.M. = 3732 and 100% N<sub>1</sub> R.P.M. = 6774 and therefore the above percent data plate speeds should be revised accordingly. i.e. increase percentage by 0.20%



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2) ADEQUACY OF INSTRUMENTATION FOR THRUST MEASUREMENT

A list of available instrumentation which can be used for thrust measurement during Arrow 1 flight tests is given under report 71/PERF/2 (sheets 2 & 3). Complete engine instrumentation is not available and therefore certain estimations, based on manufacturer's figures for basic engine performance (Charts 3 & 4 Report 71/PERF/2) and on Avro Nobel Test results and a NACA method for ejector performance (Charts 6 & 7 Report 71/PERF/2) must be used to complete the calculations. In addition to using the above manufacturer's data for basic engine performance, their data must also be used to derive final nozzle total pressure  $P_{10}$ , and total temperature  $T_{10}$ , from measured quantities at the engine inlet and turbine outlet, for use in obtaining installed gross thrust (with ejector) values.

Primary engine gross thrust determination depends on turbine outlet total pressure,  $P_7$ , measurement which is adequately measured by manifolded rake measurements. Primary engine momentum drag depends on compressor inlet  $P_2$  (total pressure) and  $p_2$  (static pressure) measurements; the former being adequately measured by 2 or 3 representative probes (after rake calibration while the latter is measured by a single wall static vent mounted on the inboard side on the centre line of the inlet duct approx. 6 feet upstream of the L.P. compressor face. This static vent pressure measurement is primarily used for structural loading investigations and can be used to represent static pressure at the engine face for momentum drag consideration since relative areas should be the same (after allowing for aft diffusing and nose bullet). However, approx. 3% total air weight flow is extracted to the overboard cooler just upstream of the compressor face and therefore the static pressure measurement should be increased approx. 1% to be more representative of the pressure at the compressor face. (See table 1)

Determination of installed gross thrust (with ejector) requires the measurement of air weight flow and total temperature at the by-pass exit. For this, measurements of  $p_B$ ,  $T_B$  and  $P_B$  are obtained by various means. i.e. Static pressure,  $p_B$ , is measured near the by-pass exit relative to ambient static pressure,  $p_1$ . Absolute  $p_B$  can therefore be readily obtained by adding  $p_1$  to  $(p_B - p_1)$ . Total by-pass temperature,  $T_B$ , is measured upstream of  $p_B$  and assumed equal to  $T_B$  near exit. Total pressure,  $P_B$ , is measured further upstream (approx. mid jet pipe) but is actually a static pressure measurement. Since the by pass area is large at this station a relatively low mean Mach number of .31 will be assumed such that measured mid jet pipe  $p_B \approx P_B/1.07$ . Measurements of  $P_B$  &  $p_B$  are made by single probes while  $T_B$  is measured on two probes, one above and one below the jet pipe. Disadvantages of single or dual probe measurements compared to rake measurements for average readings are well known and therefore care must be exercised in interpreting the results. (see table 2) By-pass measurements are only made on the port engine and identical readings will be assumed for the starboard side. Programming for performance data from Arrow 1 flight tests according to report 71/PERF/2 is therefore valid only for symmetrical power conditions.



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Geometric areas must be measured at the reference stations (by-pass exit and engine face inlet) and then corrected to an effective area using an estimated coefficient for use in appropriate air weight flow formulae. Air weight flows will be obtained as an output from IBM 704 computations as well as final net thrust. If these air weight flows do not reasonably agree with estimates (due to inadequate instrumentation) the area coefficients or pressure measurement coefficients can be adjusted such that a good measure of thrust is obtainable which should be consistent for all flights using the same instrumentation. A preliminary estimate of area coefficients is .97 and .93 for engine face and by-pass exit respectively. Probable tolerance on these area coefficients is approximately .025.

In conclusion, it is stated that a reasonable or consistent measure of thrust is expected from available instrumentation. Some deterioration in thrust measurement accuracy is expected at the lower engine powers at high altitude (low ambient static pressure) due to inadequate instrumentation. Use of two or three range pressure measurement instrumentation at the engine face and at the turbine outlet would improve overall accuracy.





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ENGINE PERFORMANCE

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TABLE 1 EFFECT OF INSTRUMENTATION ACCURACY ON DETERMINATION OF AIR WEIGHT FLOW AND MOMENTUM DRAG AT ENGINE FACE

Note: 1)  $\dot{W}_E = \rho_E A_2 V_2 = \frac{P_2}{Rt_2} \times A_2 \times M_2 \times \sqrt{\gamma g R t_2} =$

$$= \sqrt{\frac{\gamma g}{R t_2}} \times P_2 A_2 M_2$$

where "static  $t_2$ " = "total  $T_2$ "  $\left(\frac{P_2}{P_2}\right)^{\frac{\gamma-1}{\gamma}} = T_1 \left(\frac{P_2}{P_2}\right)^{.286}$

2)  $\dot{m}_E V = \frac{\dot{W}_E \times V}{g}$  where  $V$  = free stream velocity

$$3) M_2^2 = \left[ \left(\frac{P_2}{P_2}\right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \times \frac{2}{\gamma-1} = 5.0 \left[ \left(\frac{P_2}{P_2}\right)^{.286} - 1 \right]$$

For 1% error in pressure measurement at engine face

$$M_2 = .5 \text{ tolerance} = \pm .015 = \pm 3.0\%$$

$$M_2 = .4 \text{ tolerance} = \pm .019 = \pm 4.75\%$$

$$M_2 = .3 \text{ tolerance} = \pm .025 = \pm 8.3\%$$

Hence if  $P_2$  measurement is in error by  $\pm 1\%$  then  $t_2$  will be error

$$\pm .143\% \text{ and } \dot{W}_E \text{ and } \dot{m}_E V \text{ will be in error } \pm 3.14\% \text{ at } M_2 = .5$$

$$\pm 4.89\% \text{ at } M_2 = .4$$

$$\pm 8.44\% \text{ at } M_2 = .3$$

If  $p_2$  measurement is in error by 1% the effect on  $\dot{W}_E$  and  $\dot{m}_E \times V$  will be similar to that for  $P_2$  but with the absolute value of the error reduced by 1%.



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TABLE II EFFECT OF INSTRUMENTATION ACCURACY ON DETERMINATION OF  
AIR WEIGHT FLOW AT BY-PASS EXIT

NOTE:- 1)  $\dot{W}_B = \rho_B A_B V_B = \frac{P_B}{Rt_B} \times A_B \times M_B \times \sqrt{\gamma g R t_B}$

$$= \sqrt{\frac{\gamma g}{R t_B}} P_B A_B M_B$$

$$2) M_B^2 = \left[ \left( \frac{P_B}{P_B} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \frac{2}{\gamma-1} = 5.0 \left[ \left( \frac{P_B}{P_B} \right)^{.286} - 1 \right]$$

For 1% error in pressure measurement

$$M = 1.0 \text{ tolerance} = \pm .009 = \pm 0.9\%$$

$$M = 0.8 \text{ tolerance} = \pm .010 = \pm 1.25\%$$

$$M = 0.6 \text{ tolerance} = \pm .013 = \pm 2.2\%$$

Hence if  $P_B$  measurement is in error by  $\pm 1\%$

Then  $\dot{W}_B$  will be in error  $\pm 1.04\%$  at  $M_B = 1.0$

$$\pm 1.39\% \text{ at } M_B = 0.8$$

$$\pm 2.34\% \text{ at } M_B = 0.6$$

If  $P_B$  measurement is in error by 1% the effect on  $\dot{W}_B$  will be similar to that for  $P_B$  but with the absolute value of the error reduced by 1%.

Any error in  $T_B$  measurement causes an error in  $\dot{W}_B$  which is inversely proportional to  $\sqrt{T_B}$ .

## 3) THRUST MEASUREMENT TECHNIQUE

The following symbols are used in the derivation of ensuing formulae:-

capital T = total temperature °K

capital P = total pressure

small p = static pressure

F = installed engine thrust (with extractor)

X = basic or primary engine thrust



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subscript G = gross  
" N = net  
" 1 = station 1, free stream  
" 2 = " 2, engine face  
" 7 = " 7, turbine outlet  
" 10 = " 10, final nozzle (primary)  
" B = " 10, in by-pass

Primary engine gross thrust is derived from turbine discharge total pressure measurement as follows:-

$$X_G = \left[ 1.255 \frac{P_7}{P} - 1 \right] C_g \times A_{10} p \text{ for } \frac{P_7}{P} \geq 1.852 \quad (1)$$

$$X_G = 8.06 \left[ \left( \frac{P_7}{P} \right)^{.248} - 1 \right] C_g \times A_{10} p \text{ for } \frac{P_7}{P} < 1.852 \quad (2)$$

for  $\gamma = 1.33$  and  $p$  = ambient static pressure

Effect of  $\gamma = 1.33$  down to approx. 1.30 for afterburner operation has negligible effect on the above formulae. (See also P.W.A. Curve No. Inst. 16624).

Nominal  $A_{10} = 3.68$  sq.ft. = 530 sq.inches (cold and relaxed) A/B off  
= 6.398 sq.ft. = 921 sq.inches (est. operating) A/B on

However  $A_{10}$  values, based on P.W.A. engine test bed calibration runs on engines for A/C No. 1 = 510 ( $\pm 2$ ) sq.inches A/B off  
= 928 (+ 19) sq.inches A/B on  
(- 11)

$C_g$  = gross thrust coefficient from P.W.A. curve no inst. 27214 and 18151.

To cover engine idling cases at low altitude curve 27214 for A/B off must be extended downward to  $P_{7/p} \approx 1$  where  $C_g$  will then be approximately .80 based on data from log book of engines 610026 and 610027 (See charts III and IV of report 71/PERF/2).

To determine primary net thrust, momentum drag to the engine proper must be subtracted from  $X_G$  to obtain  $X_N$ . Total and static pressure are measured at or near the engine face and therefore momentum drag is determined from the formulae:-

$$m_E^V = A_2 p_2 \left( \frac{2}{\gamma-1} \right) \sqrt{\left[ \left( \frac{P_2}{P_2} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \times \left[ 1 - \left( \frac{p}{P} \right)^{\frac{\gamma-1}{\gamma}} \right]} = \frac{W_E \times 65.8 \sqrt{T_0}}{g}$$

where  $A_2$  = geometric area at engine face corrected by an area coefficient





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The next stage in thrust measurement consists of determining net thrust of the complete engine installation including intake duct and ejector.

Total gross thrust,  $F_G$ , is determined from the ratios  $\frac{F_G}{X_{iG}}$  for A/B off  $\frac{F_G}{X_G}$  for A/B on, where  $X_G$  is the primary gross thrust as previously determined and  $X_{iG}$  is an ideal primary gross thrust.

Ideal primary gross thrust assumes isentropic expansion to ambient pressure behind the final nozzle and is determined as follows

$$X_{iG} = m_{10} \sqrt{\frac{2 \gamma R_g T_{10}}{\gamma - 1} \left[ 1 - \left( \frac{p}{P_{10}} \right)^{\frac{\gamma - 1}{\gamma}} \right]}$$

Now for the momentum gross thrust  $(mV)_{10}$  in the final nozzle, ambient  $p$  in the above formula is substituted by final nozzle  $p_{10}$ , and for choked flow  $\left( \frac{P_{10}}{p} \geq 1.252 \right)$ ,  $M_{10} = 1$  and  $P_{10} = \left( \frac{2}{\gamma + 1} \right)^{\frac{\gamma}{\gamma - 1}} \times P_{10}$

$$\text{Then } \frac{X_{iG}}{(mV)_{10}} = \sqrt{\frac{1 - \left( \frac{p}{P_{10}} \right)^{\frac{\gamma - 1}{\gamma}}}{\frac{\gamma - 1}{\gamma + 1}}} = 2.66 \sqrt{1 - \left( \frac{p}{P_{10}} \right)^{.243}}$$

for  $\gamma = 1.33$

Now equation (1) can be rearranged such that

$$\frac{X_G}{(mV)_{10}} = \frac{1.255 \frac{P_{10}}{p} - 1}{.714 \frac{P_{10}}{p}}$$

$$\text{Hence } \frac{X_{iG}}{X_G} = \frac{1.90 \frac{P_{10}}{p} \sqrt{1 - \left( \frac{p}{P_{10}} \right)^{.243}}}{1.255 \frac{P_{10}}{p} - 1}$$

See Chart V  
Report 71/Perf/2

(3)



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This equation is used for A/B off only, for which it can be assumed that  $P_{10} = .99 P_7$  (where  $P_7$  is measured).

The ratios  $\frac{F_G}{X_{iG}}$  and  $\frac{F_G}{X_G}$  are obtained from experimental data

i.e. for A/B off, a NACA solution is used (Chart VI of 71/Perf/2) and for A/B on, Avro Nobel Test results are used (Chart VII of 71/Perf/2)

To determine  $\frac{F_G}{X_{iG}}$  and  $\frac{F_G}{X_G}$  values of  $\frac{P_{10}}{p}$  and  $\mu$  must be known.

$\frac{P_{10}}{p}$  must be derived from measured  $\frac{P_7}{p}$ , which for A/B off

=  $.99 \frac{P_7}{p}$  (as above) while for A/B on,  $\frac{P_{10}}{p}$  is derived as follows:-

According to J T 4A Engine Installation Handbook

$P_{10} = 0.1297 X_G + 0.8 p$  for A/B on, and if  $A_{10} = 6.398$  sq.ft., then  $\frac{X_G}{.965 A_{10} p} = 1.250 \frac{P_{10}}{p} - 1$

It is therefore evident that a nozzle coefficient, based on  $\frac{P_{10}}{p}$ , of .965 was used.

Now  $C_g$  (Chart IV Report 71/Perf/2) is based on  $\frac{P_7}{p}$ ; and the difference between  $C_g$  and .965 is assumed to account for the pressure loss from  $P_7$  to  $P_{10}$

$$\therefore \frac{X_G}{C_g A_{10} p} + 1 = 1.250 \frac{P_7}{p} \quad (\text{based on } P_7)$$

$$\text{and } \frac{X_G}{.965 A_{10} p} + 1 = 1.250 \frac{P_{10}}{p} \quad (\text{based on } P_{10})$$

Solving these two equations

$$\frac{P_{10}}{p} = \frac{C_g}{.965} \times \frac{P_7}{p} - \frac{C_g}{1.206} + 0.8 \quad \text{--- (4)}$$





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For evaluation of  $\mu$  which equals  $\frac{W_B}{W_{10}} \sqrt{\frac{T_B}{T_{10}}}$  the following assumptions are made:

- a).  $W_B$  (lbs/sec) and  $T_B$  ( $^{\circ}K$ ) are air weight flow and total temperature as measured in the by-pass near the final nozzle.

$$W_B = \frac{P_B^{A/B} \sqrt{g}}{\sqrt{RT_B} \left( \frac{P_B}{P_B} \right)^{\frac{\gamma-1}{\gamma}}} \sqrt{\frac{2\gamma}{\gamma-1} \left[ 1 - \left( \frac{P_B}{P_B} \right)^{\frac{\gamma-1}{\gamma}} \right]} = \frac{P_B^{A/B} \sqrt{g}}{\sqrt{RT_B} \left( \frac{P_B}{P_B} \right)^{.286}} \sqrt{7 \left[ 1 - \left( \frac{P_B}{P_B} \right)^{.286} \right]} \quad (5)$$

for  $\gamma = 1.4$ ,  $R = 96.02$

- b)  $W_{10}$  = air weight flow through the primary nozzle, which for the A/B off case is assumed = engine inlet  $W_E$  and for the A/B on case is assumed =  $W_E + \frac{Q_{A/B}}{3600}$  (A/B fuel flow, lbs/hr) i.e. engine fuel flow (approx 2.5% of  $W_E$ ) is assumed to offset airbleed & leakage

$$W_E = \frac{P_2 A_2 \sqrt{g}}{\sqrt{RT_2} \left( \frac{P_2}{P_2} \right)^{.286}} \sqrt{7 \left[ 1 - \left( \frac{P_2}{P_2} \right)^{.286} \right]} \quad \text{for } \gamma = 1.4, R = 96.02 \quad (6)$$

$$b) \quad T_{10} = T_7 \text{ (}^{\circ}K\text{) for A/B off and } \sqrt{T_{10} \text{ (}^{\circ}K\text{)}} = \left[ \frac{.745 \times X_G}{W_E + \frac{Q_{A/B}}{3600}} \right] \times \left[ \frac{.0009 \left( \frac{X_G}{P} \right) + 0.8}{.00219 \left( \frac{X_G}{P} \right) - .02} \right] \quad \text{for A/B on (p in psi)} \quad (7)$$

Formula (7) is obtained by combining two equations from J.T.4A Engine Installation Handbook and letting  $W_{10} = W_E + \frac{Q_{A/B}}{3600}$

$$\text{i.e. Combine } T_{10} = \left[ \frac{X_G / W_{10}}{2.435 - 1.897 \frac{p}{P_{10}}} \right]^2 \quad \text{for } T_{10} \text{ in } ^{\circ}R, \text{ with } P_{10} =$$

$0.1297 X_G + 0.8 p$  for p in psf.



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To derive installed net thrust (excluding external pressure drag around ejector), momentum drag and spillage drag must be subtracted from installed gross thrust.

$$i.e. F_N = F_G - m_v - D_S$$

Momentum drag,  $m_v$ , is determined by mass flow measurements at the engine face, to which is added the mass flow as measured in the by-pass near the exit and then multiplied by airplane velocity.

$$i.e. m_v = \frac{(W_E + W_B) M \times 65.8 \sqrt{T_0}}{32.2}$$

where  $W_E$  is obtained from equation (6) .

$W_B$  is obtained from equation (5).

$M$  = true Mach number

$T_0$  = true ambient air temperature °K

It should be noted that

1.  $W_B$  is airflow that enters through the by-pass doors and/or through the blow in doors. It is assumed that air entering the blow in doors (at low Mach number, low altitude) is extracted from the free stream at free stream velocity.

2. Airflow through the inlet duct to the overboard oil cooler is neglected since this airflow is less than 3% of total air flow, and approximately 50% of the momentum drag of the oil cooler air flow, is regained as thrust at the overboard cooler exit. The effect therefore is less than 1 1/2% on total momentum drag and less than .75% on net thrust.

Intake spillage drag is not directly measureable, except by suitable flight tests such as accelerated levels at various engine settings, and hence wind tunnel data will be used. This data may change as the tests progress. Intake spillage drag data is presented as curves of  $\frac{D_{DS}}{\frac{P_{th}}{F_1}}$  and  $\frac{D_{DS}}{\frac{m_1}{m_0}}$

versus  $M$  ( see chart VIII & IX Report 71/PERF/2 Issue 2 )

$$\text{where } C_{DS} = \text{spillage drag coefficient} = \frac{D_S}{\frac{\gamma}{2} \rho M^2 S} = \frac{D_{DS}}{\frac{\gamma}{2} \rho \left( \frac{m_1}{m_0} \right)} \left( \frac{m_1}{m_0} - \frac{m_1}{m_1} \right)$$

$S$  = area = 40.98 sq.ft.

$p$  = ambient static pressure

$M$  = Mach number

$m_1$  = actual inlet air weight flow

= air flow to engine,  $W_E$ , as measured

+ air flow in by-pass,  $W_B$ , as measured

+ air flow to overboard cooler,  $W_C$ , (assume mean value = 5 lb/sec.)

$m_1$  = inlet air weight flow corresponding to choked conditions at the throat

$m_0$  = nominal or capture air weight flow



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Adding  $W_B$  and  $W_C$  to  $W_E$  to obtain  $m_1$  is not valid when the by-pass doors are closed. This only occurs at low altitude, low Mach number and therefore is unimportant for spillage drag considerations.

Now effective inlet throat area =  $.97 \times 5.6 = 5.43$  sq.ft.  
and capture area =  $10.18$  sq.ft.

Hence:-

$$m_o = \rho_{AV} = \frac{p}{RT_o} \times 10.18 \times 65.8 M \sqrt{T_o} = 6.97 \frac{pM}{\sqrt{T_o}} \text{ for } p \text{ in psf}$$

and  $T_o$  (amb. static temp.) in  $^{\circ}K$

$$\begin{aligned} m_1^* &= (\rho_{AV})_{throat} = \left( \frac{p}{Rt} \right)_{th.} \times 5.43 \times 65.8 (M \sqrt{t})_{th.} \text{ where } t = \text{static temp.} \\ &= 1.962 \frac{P_{th}}{\sqrt{t_{th}}} \text{ for } M_{th} = 1, P_{th} = 1.894 P_1 \text{ \& } R = 96.02 \\ &= 1.962 \frac{P_1}{\sqrt{t_{th}}} \left( \frac{P_{th}}{P_1} \right) \end{aligned}$$

$$\text{Now } T_o (1 + .2M^2) = t_{th} (1 + .2M^2)_{th} = 1.2 t_{th}$$

$$\text{Hence } \frac{m_1^*}{m_o} = \frac{1.962 P_1}{6.97 pM} \left( \frac{P_{th}}{P_1} \right) \times \sqrt{\frac{1.2 T_o}{(1 + .2M^2) T_o}} = \frac{.308 (1 + .2M^2)^3}{M} \left( \frac{P_{th}}{P_1} \right)$$

Therefore, spillage drag can be evaluated knowing  $W_E$ ,  $W_B$ ,  $p$ ,  $M$ ,  $T_o$  and using charts VIII & IX of Report 71/PERF/2 Issue 2.

Installed net thrust can then be compared to primary net thrust as determined previously, in order to verify installation effects. The latter thrust is also useful for comparison to engine brochure curves (after correcting for ambient temperature to standard, intake pressure recovery power extraction and air bleed) and should be more reliable since it will have been based on P.W.A. approved thrust coefficients and turbine outlet and engine face total pressure measurements but with the exception of unapproved static pressure measurement at the engine face.



AVRO AIRCRAFT LIMITED  
MALTON ONTARIO

# TECHNICAL DEPARTMENT

AIRCRAFT

ARROW 1

A/C No. 1

E.GINE PERFORMANCE

REPORT NO 70/PERF/1 APP.II

SHEET NO 12

PREPARED BY

DATE

R. Waechter

Oct. 1957

CHECKED BY

DATE

## CORRECTED ENGINE PERFORMANCE (ARROW 1 A/C No.1)

(P.W.A. RUN IN AND FINAL ACCEPTANCE ENGINE TEST. BED CALIBRATIONS)

Engine:- 610034 (port)

Power	$F_N$	$N_2$	$N_1$	T.S.F.C.	$T_{T_1}$	$P_{T_1}/P_{T_2}$	$N_2$ Data Plate Speed (IAS 60°) R.P.M.
Military	15,500	8630	6630	.792	1057	2.50	8645 at 98.30%
Normal	13,730	8380	6250	.759	947	2.33	
75% Norm.	10,300	7940	5550	.726	782	1.99	

Engine:- 610029 (stbd.)

Military	15,500	8690	6640	.797	1073	2.51	8710 at 99.55%
Normal	13,780	8450	6280	.757	960	2.34	
75% Norm.	10,300	8020	5600	.728	837	1.93	

Engine:- 610026 (spare)

Military	15,500	8690	6670	.733	1068	2.49	8725 at 99.72%
Normal	13,730	8445	6310	.760	950	2.33	
75% Norm.	10,300	7955	5580	.733	790	2.01	

Engine:- 610027 (spare)

Military	15,500	8715	6715	.806	1065	2.51	8725 at 99.72%
Normal	13,780	8450	6335	.775	965	2.35	
75% Norm.	10,300	7915	5560	.737	815	2.02	

Note:- Percentage ( $N_2$ ) R.P.M.'s based on 8750 as 100%

Average Military  $N_1$  = .763  $N_2$





AVRO AIRCRAFT LIMITED  
MALTON - ONTARIO

TECHNICAL DEPARTMENT

REPORT NO. 70/PERF/1 APP. II

SHEET NO 13

AIRCRAFT:

ARROW 1

ENGINE PERFORMANCE

A/C 1

PREPARED BY

DATE

R. Waschter

Oct. 1957

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AFTERBURNER PERFORMANCE

Y J 75 P - 3 ENGINE FOR ARROW 1 A/C No. 1

(P.W.A. RUN IN AND FINAL ACCEPTANCE ENGINE TEST BED CALIBRATIONS)

Engine:- 610034(port)

Power	Corr. $F_N$	Obs. $N_2$	T.S.F.C.	BIAS.T.S.F.C.	$T_{T_2}$ (°F)
Mil. Non A/B	16,840	3600	.327	-	32
Afterburner	25,520	3610	1.933	1.945	32

Engine:- 610029 (stbd)

Mil. Non A/B	16,630	3670	.320	-	33
Afterburner	25,220	3665	1.92	1.93	32

Engine:- 610026 (spare)

Mil. Non A/B	17,030	3690	.324	-	32
Afterburner	26,000	3685	1.90	1.915	31

Engine:- 610027 (spare)

Mil. Non A/B	16,675	3700			40
Afterburner	25,150	3695	1.94	1.95	40





AVRO AIRCRAFT LIMITED  
MALTON - ONTARIO

# TECHNICAL DEPARTMENT

REPORT NO 70/PERF/1 APP.II

SHEET NO 14

AIRCRAFT

ARROW 1  
A/C No. 1

ENGINE PERFORMANCE

PREPARED BY

DATE

R. Waechter

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DATE

## DETERMINATION OF "AERODYNAMIC" NOZZLE AREA

Y J75 P - 3 ENGINES FOR ARROW 1 A/C No. 1

P.W.A. RUN IN AND FINAL ACCEPTANCE TEST BED CALIBRATIONS

Assumptions 1)  $\frac{X_G}{C_g A_{10} p} = 1.255 \frac{P_7}{p} - 1$

or  $A_{10} = \frac{X_G / (C_g \times p)}{1.255 \frac{P_7}{p} - 1}$

2)  $\frac{P_7}{p} = \frac{P_7}{P_2}$  and  $\frac{X_G}{p} = \frac{F_N}{14.7 \delta_{T2}}$

3) At same  $N_2$ ,  $\frac{P_7}{P_2}$  A/B on =  $P_7/P_2$  A/B off

4)  $C_g$  from 71/PERF/2 Chart III A/B off  
Chart IV A/B on

5) P.W.A. Final Acceptance Test Bed Calibrations  
have been corrected to standard sea level conditions

Note:-

1) Nominal  $A_{10}$  for Y J75 P - 1, 3 and 11 engines

= 530 sq.in. (A/B off)  
= 921 sq.in. (A/B on)

2)  $A_{10}$  values are calculated at actual test points



AVRO AIRCRAFT LIMITED  
MALTON - ONTARIO

# TECHNICAL DEPARTMENT

REPORT NO 70/PERF/1 APP. II

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AIRCRAFT:

ARROW 1  
A/C No. 1

## ENGINE PERFORMANCE

PREPARED BY

DATE

R. Waechter

Oct. 1957

CHECKED BY

DATE

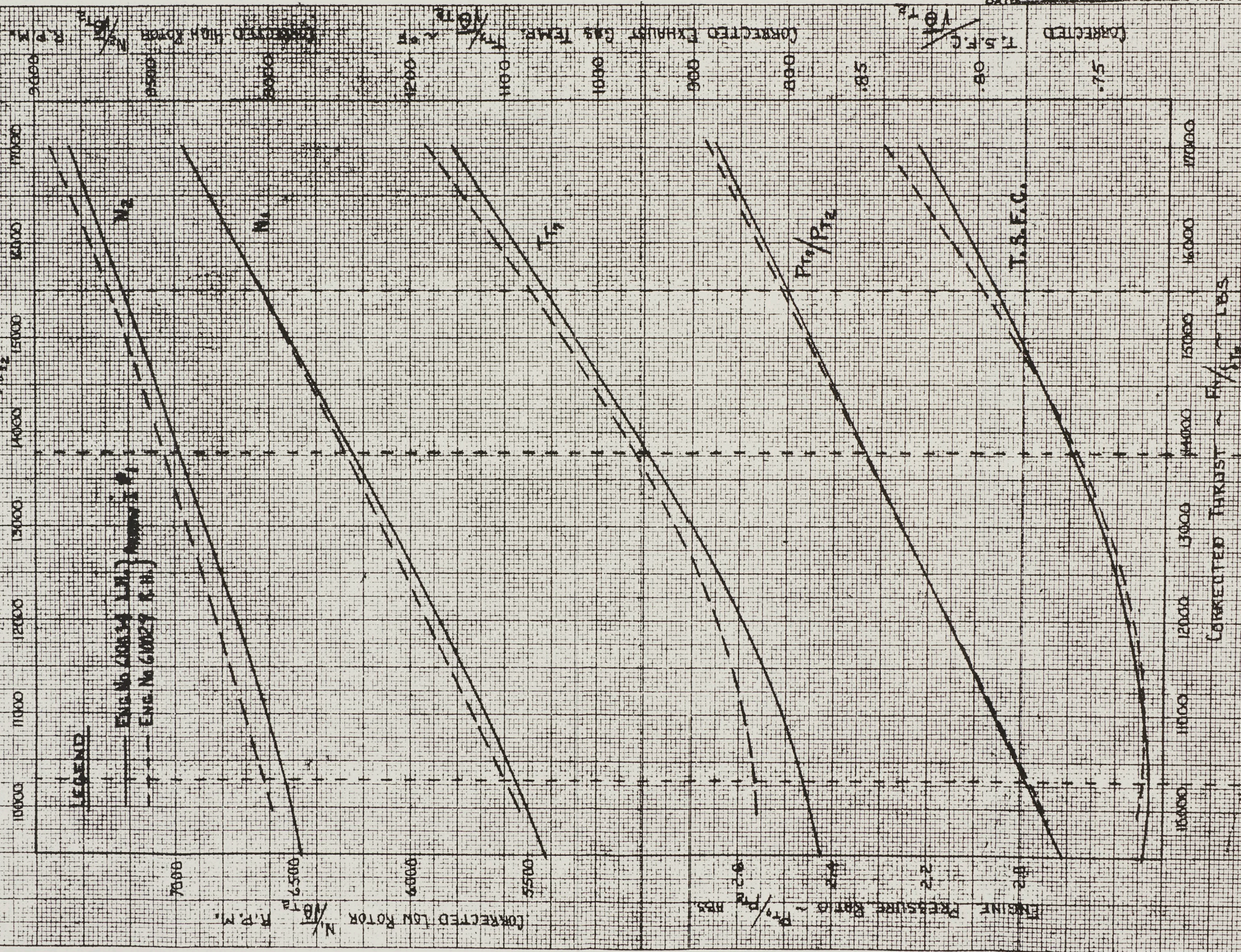
Engine	$\frac{F_N}{\sigma T_2} = \frac{14.7 X_G}{P_2}$	$\frac{P_7}{P_2}$	$\frac{X_G}{C_g A_{10} P_2}$	$C_g$	$\frac{X_G}{A_{10} P_2}$	14.7 A <sub>10</sub>	A <sub>10</sub> □ "	A <sub>10</sub> (aver.)
610026 (spare)	9,860 12,150 12,180 14,400 15,200 16,570 17,120	1.950 2.131 2.150 2.400 2.470 2.600 2.640	1.445 1.737 1.700 2.010 2.100 2.260 2.310	.910 .937 .935 .959 .963 .973 .976	1.317 1.628 1.591 1.929 2.022 2.201 2.258	7490 7400 7650 7460 7510 7520 7580	509 508 521 507 511 512 516	512 □ "
610027 (spare)	10,390 12,420 12,610 14,310 15,210 16,630 16,790	1.988 2.220 2.230 2.430 2.480 2.630 2.639	1.495 1.785 1.800 2.050 2.110 2.300 2.310	.903 .940 .942 .960 .966 .974 .975	1.351 1.678 1.697 1.970 2.040 2.241 2.255	7690 7400 7430 7520 7450 7420 7445	523 503 505 512 507 505 507	509 □ "
610029 (stbd)	10,500 11,730 12,670 14,300 14,800 16,650 16,650	2.016 2.120 2.235 2.441 2.441 2.630 2.630	1.530 1.660 1.805 2.063 2.063 2.300 2.300	.913 .930 .943 .962 .962 .974 .974	1.398 1.544 1.702 1.987 1.987 2.241 2.241	7500 7590 7430 7440 7440 7420 7420	510 516 506 506 506 505 505	508 □ "
610034 (port)	9,540 11,330 11,830 14,110 15,000 16,510 16,880	1.910 2.150 2.150 2.370 2.450 2.616 2.639	1.395 1.700 1.700 1.975 2.075 2.280 2.310	.905 .935 .935 .956 .963 .974 .975	1.263 1.590 1.590 1.890 1.999 2.221 2.254	7550 7450 7450 7460 7500 7430 7430	513 507 507 508 510 506 509	508 □ "
610026	26,000 A/B On	2.635	2.305	.809	1.867	13920	947	932 □ "
610027	25,150 " "	2.634	2.305	.809	1.867	13480	917	
610029	25,220 " "	2.630	2.300	.809	1.862	13540	921	
610034	25,520 " "	2.639	2.310	.809	1.871	13630	928	



# Y195 P-3 PERFORMANCE CURVES

FINAL ACCEPTANCE TESTS

CORRECTED THRUST ~  $F_{T_2}$  ~ LBS



75% NORM. NORTH MILITARY

SECRET



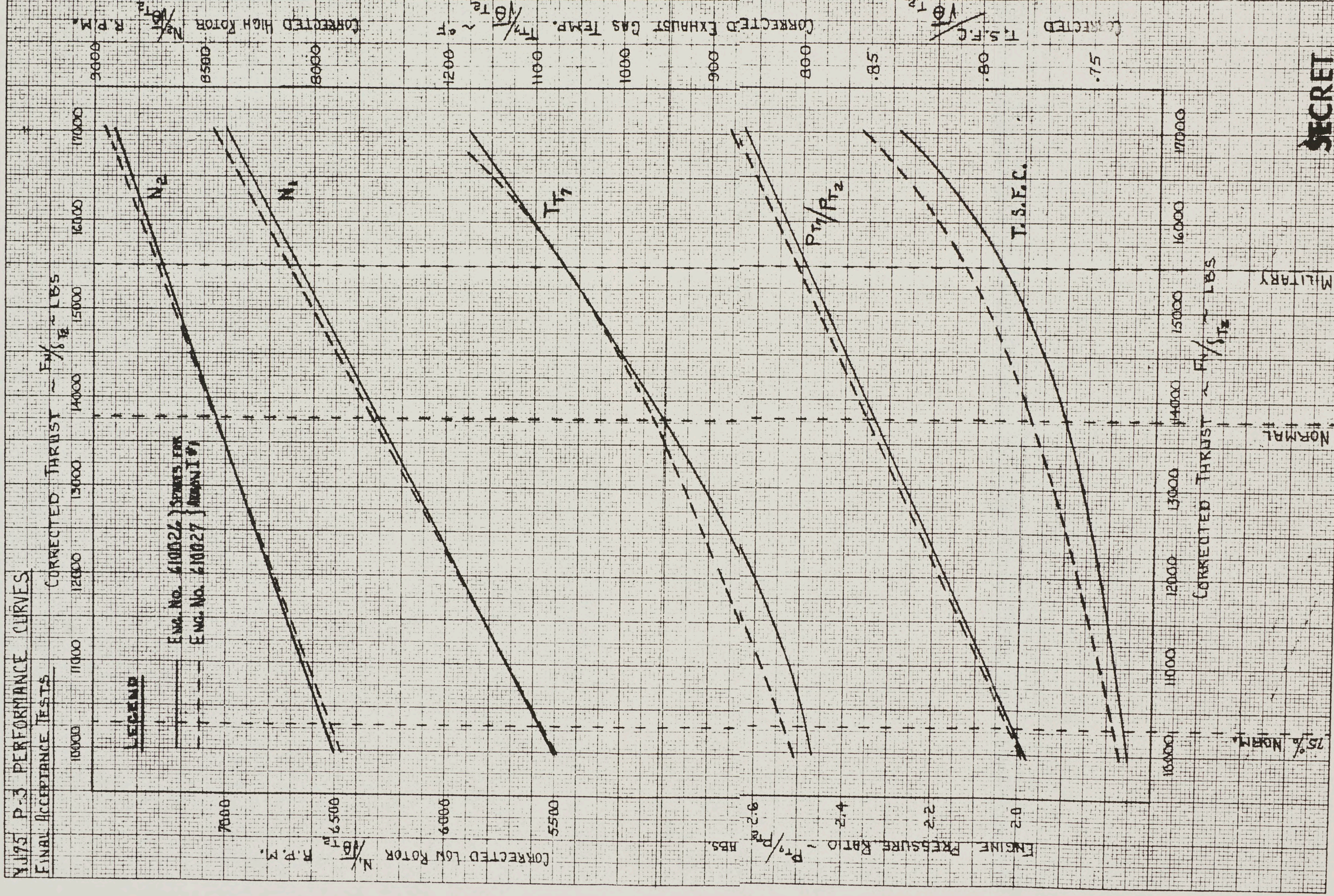
# YJ75 P-3 PERFORMANCE CURVES

FINAL ACCEPTANCE TESTS

CORRECTED THRUST ~  $F_N / \sqrt{\sigma_2}$  ~ LBS

## LEGEND

ENG. NO. 610026 } SPEEDS FOR  
ENG. NO. 210027 } ACCEPTANCE



SECRET

SHEET NO. 17  
DATE OCT. 1957

REPORT NO. 90/PREF/1 APP. II  
PREP BY R. W. WRIGHT